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## The formation young's modulus and textural attributes of the Axx-field from southern Niger delta, Nigeria

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### Abstract

This research was carried out to determine the formation brittleness and textural attributes of an Axx-Field in the Niger Delta Basin. Data available for this study were obtained from three wells (A11, A22 and A33). They were analyzed using Microsoft Excel after spurious values were removed. Two techniques (John Fuller and Plumb Bradford) were used to determine static young's modulus but only one is reported because after statistical analysis on both, the one reported was adequate for accurate outcomes although both approaches have low variance. The results indicates that the highest values of static and dynamic young's modulus are  $2.05 \times 10^{25} \text{N/m}^2$  and  $1.93 \times 10^{10} \text{N/m}^2$  respectively. The lowest values are  $1.1 \times 10^{24} \text{N/m}^2$  and  $8.5 \times 10^9 \text{N/m}^2$  respectively for well A11. The average values are  $1.024 \times 10^{25} \text{N/m}^2$  and  $5.25 \times 10^{23} \text{N/m}^2$  for this well. For well A22, the highest and lowest values of dynamic young's modulus are  $1.5848 \times 10^{10} \text{N/m}^2$  and  $1.5726 \times 10^{10} \text{N/m}^2$  while those of static are correspondingly  $1.47 \times 10^{25} \text{N/m}^2$  and  $9.01 \times 10^{14} \text{N/m}^2$ . Their average values are  $1.5787 \times 10^{10} \text{N/m}^2$  and  $7.35 \times 10^{24} \text{N/m}^2$  for dynamic and static young's moduli respectively. Also, for well A33, dynamic has the lowest value as  $3.28 \times 10^{10} \text{N/m}^2$ ; static has  $8.36 \times 10^{14} \text{N/m}^2$  and their highest correspond to  $2.04 \times 10^{10} \text{N/m}^2$  and  $7.08 \times 10^{25} \text{N/m}^2$ . The average value for this well are  $2.66 \times 10^{10} \text{N/m}^2$  and  $3.54 \times 10^{25} \text{N/m}^2$  for dynamic and static respectively. The static Young's modulus results define the formation as brittle, whose environment is extremely poorly sorted, very fine skewed and very leptokurtic with low energy for well A11, very poorly sorted, fine skewed and platykurtic for well A22, extremely poorly sorted, very fine skewed and mesokurtic for well A33.

**Keywords:** Young's modulus; Gamma ray; Textural parameters; Sorting; Skewness; Percentile; Velocity; Shear modulus

### 1 Introduction

Brittleness defines the property of a material that fractures when it is stressed but has a slight tendency to deform before rupture (Zhang, 2011). Young's modulus is an elastic mechanical rock characteristic that shows a stones resistance of the layer to uniaxial load. It is one of the brittleness evaluation parameters and can be quantified through extracted rock elastic properties. Other parameters are Poisson 's ratio and lame's parameters. Young's modulus is vital in the static drilling of hydrocarbon wells since it helps to describe the formation and total stresses, which is utilized to manage well bore instability. The mechanical properties (mainly including elastic moduli and strength) of rocks play a significant role in the hydraulic fracturing of reservoirs in terms of initiating and propagating the fractures (Josh *et al.*, 2012) and thus impact both the efficiency of the fracturing methods and the flow of hydrocarbons to the well bore (Eliyahu *et al.*, 2015). Using the elastic and strength properties of rock, a variety of brittleness indices may be noted to quantitatively evaluate rock brittleness, which can be used to access the favorability of reservoirs for fracturing operation (Grieser and Bray, 2007). Brittleness is a critical indicator for hydraulic fracturing candidate screening in unconventional reservoirs. The areas with high young's modulus and low Poisson's ratio are more productive for

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hydraulic fracturing due to their high brittleness. Static young's modulus changes greatly with the different of the lithology. For shale, the static Young's modulus varies from 0.1Mpsi to 0.99Mpsi. It ranges from 8 and 12Mpsi in limestone and 2 to 10Mpsi in sandstone. These differences in young's modulus values emphasize that this characteristic changes with lithology, making it essential in prediction of the static young modulus along hydrocarbon wells. Probability of failure rises with depth in deep wells (deeper than 1500 meters).

Geomechanical properties of rocks are either statically or dynamically measured. Static measurement has to do with the use of core specimens in the laboratory, where the core specimens are exposed to incremental compression until they undergo fracture while recording the stress-strain curve. The dynamic mechanical properties can be obtained using p-wave velocities from seismic, well logs or laboratory-analyzed core data (Al-Shayea, 2004; Hongzhi, 2005; Chang *et al.*, 2006; Xu *et al.*, 2016). To avoid frequent drilling challenges relative to wellbore stability, precise description of the geomechanical properties of a rock is necessary. Sonic and density logs may be employed in determining the dynamic mechanical properties of a reservoir rock which include bulk modulus, young's modulus, Poisson's ratio and shear modulus, in order to obtain static mechanical properties leading to the estimation of rock strength properties (Archer and Rasouli, 2012; Najibi *et al.*, 2015; Xu *et al.*, 2016). Dynamic moduli values are usually less than their equivalent static moduli, and as such the ratio of dynamic moduli to static moduli gets smaller with increasing confining pressures, while their difference increases in tight sands and shale reservoirs (Adham, 2016).

Grieser and Bray (2007), suggested a brittleness index, using young's modulus and Poisson's ratio stating that rocks with a high young's modulus and low Poisson's ratio will be brittle. Britt and Schoeffler (2009), concluded that shale with a static young's modulus larger than  $3.5 \times 10^6$  psi (approximately 20.684 Gpa) will be brittle. According to Maleki *et al.* (2014), the previous method of evaluating young's modulus by means of acoustic velocities revealed that the larger the acoustic velocity, corresponding to the larger density, the larger the elastic property of rocks. Static elastic moduli are preferred over moduli obtained using dynamic approaches (Eissa and kazi, 1988); this is based on the theory of the pseudo-static behavior of rock.

The focus of this research is on young's modulus information and textural attributes beginning from sonic log by converting the compressional interval transit time to p-wave velocities and then applying well established empirical relations (Archer and Rasouli, 2012; Słota-Valim, 2013, 2015; Jamshidian *et al.*, 2017). The clear advantage of this method over measurement of static properties directly, using uniaxial loading test is that, it is less destructive to the specimen, more cost effective and time efficient (Zhang and Bentley, 2005). The p-wave, and s-wave, velocities are the inverse of interval transit times (Brandås, 2012; Horsfall *et al.*, 2014; Schön, 2015).

### 1.1 Theoretical background

Young's Modulus or Elastic Modulus or Tensile Modulus, is the measurement of mechanical properties of linear elastic solids like rods, wires, and other which include Bulk modulus and Shear modulus but the value of Young's Modulus is mostly used. This is due to the fact that it gives information about the tensile elasticity of a material. Mathematically, Young's modulus (E) may be expressed as in Equation 1.

$$E = \frac{\text{Stress}}{\text{Strain}} \dots\dots\dots(1)$$

According to Atat *et al.* (2022,), Young's Modulus may also be determined using Equation 2.

$$E = 2\mu(1 + \sigma) \dots\dots\dots(2)$$

Where, E is young's Modulus in Pa or Nm<sup>-2</sup>  
 μ is Shear modulus  
 σ is Poisson's ratio

The value of Poisson's ratio ranges between -1 and 0.5 for most common materials. The minus sign indicates that the lateral strain is in the opposite direction to the axial strain.

A Poisson's ratio of 0 means that the material does not change in lateral dimensions when stretched or compressed. A positive value indicates that the material tends to expand laterally when stretched, while a negative value indicates that the material tends to contract laterally when stretched. Poisson's ratio is an important parameter in materials science and engineering, as it influences the material's mechanical behavior, such as its stiffness, deformability, and response to stress and strain.

Poisson’s ratio may be determined using Equation 3 (Atat *et al.*, 2020a; 2020b; Atat and Umoren 2016; Atat *et al.*, 2023).

$$\sigma = \frac{\left(\frac{V_p}{V_s}\right)^2 - 2}{2\left(\frac{V_p}{V_s}\right)^2 - 1} \dots\dots\dots(3)$$

Where  $\sigma$  is Poisson’s ratio  
 $V_s$  is Compressional wave velocity  
 $V_s$  is Shear wave velocity

The shear modulus is a fundamental parameter that characterizes the stiffness and ability of a material to withstand deformation under shear loads. In the context of oil wells and reservoirs, the shear modulus plays a crucial role in understanding the mechanical behavior and stability of the formation rocks.

Equation 4 is adequate for shear modulus determination (Atat *et al.*, 2012; Atat and Umoren 2016; Akpabio *et al.*, 2023a).

$$\mu = \rho V_s^2 \dots\dots\dots(4)$$

$V_s$  is shear wave velocity

Bulk modulus is one of the mechanical properties used in several geoenvironmental problems (Wang *et al.*, 2022; Bock, 1993; Bell, 1996; Andhumoudine *et al.* 2021; Yang and Liu, 2021) and it could be obtained by the stress-strain relation (like static measurement) or the propagating elastic wave velocities (such as dynamic measurement) (Wang *et al.*, 2020).

The static bulk modulus symbolizes the mechanical firmness of subsurface basins (Zimmer, 2004; Zoback, 2007). The dynamic moduli can be examined from seismic or well logging data (Fjaer, 2019; Wang *et al.*, 2022). It may be determined using Equation 5.

$$K = \frac{E}{3(1-2\sigma)} \dots\dots\dots(5)$$

$K$  is Bulk modulus (Atat *et al.*, 2020a)  
 $\sigma$  is the Poisson ratio  
 $E$  is the young’s modulus

The Statistical/textural parameters include graphic mean, graphic standard deviation, graphic skewness and graphic kurtosis. They are required for grain size and statistical spreading. Textural parameters can be obtained from percentile deduction and statistical analysis of data. It relates with the velocity of the medium accountable for the transportation and deposition of sediment (or sand-shale lithology in this research) (Atat *et al.*, 2018; Oladipo *et al.*, 2018). Table 1 highlights different interpretation of these parameters with their corresponding values.

The mean (M) may be obtained using Equation 6.

$$M = \frac{1}{3}(\phi_{16} + \phi_{50} + \phi_{84}) \dots\dots\dots(6)$$

Parameters such as standard deviation, sorting, skewness and kurtosis can be calculated using Equations 7 to 10 correspondingly.

Standard deviation (SD) is a measure of sorting. The sorting (S) of a given population is a measure of the range of grain-size present and the magnitude of these sizes around the mean sizes. SD and S expressions are presented in Equations 7 and 8 respectively.

$$SD = \frac{1}{4}(\phi_{84} - \phi_{16}) \dots\dots\dots(7)$$

$$S = \frac{\phi_{84} - \phi_{16}}{4} + \frac{\phi_{95} - \phi_5}{6.6} \dots\dots\dots(8)$$

Negatively skewed (which is coarse skewed) defines high energy environment and positively skewed (which is finely skewed) corresponds to low energy environment.

$$S_k = 0.5 \left( \frac{\phi_{84} + \phi_{16} - 2\phi_{50}}{\phi_{84} - \phi_{16}} + \frac{\phi_5 + \phi_{95} - 2\phi_{50}}{\phi_{95} - \phi_5} \right) \dots\dots\dots(9)$$

(Atat et al., 2018; Oladipo et al., 2018; Folk and Ward, 1957; Atat et al., 2022; Adedoyin 2022; Gandhi and Raja, 2014).

Kurtosis measures the sorting ratio at the extremes of the distribution. If kurtosis is defined as platykurtic, its value is negative excess kurtosis (that is, opposite situation to the case of leptokurtic); if it is mesokurtic, kurtosis curve is observed to have uniform sorting in both tails and central position and finally leptokurtic, if its value is positive excess kurtosis (tail is better sorted than central portion). It is a quantitative measure used to describe the departure from normality of distribution. It signifies the ratio between sorting in tails and central portion of the curve. The calculation of Kurtosis could be done using Equation 10.

$$K_s = \frac{\phi_{95} - \phi_5}{2.44(\phi_{75} - \phi_{25})} \dots\dots\dots(10)$$

**Table 1** Classification of textural parameters (Atat et al., 2021; Oladipo et al., 2018; Atat et al., 2022; Wentworth, 1922)

S/N	Parameters	Range of values	Interpretation/Classification
1	Sorting	Less than 0.35	Very well sorted
2	Sorting	0.35 to 0.50	Well sorted
3	Sorting	0.51 to 0.70	Moderately well sorted
4	Sorting	0.71 to 1.00	Moderately sorted
5	Sorting	1.01 to 2.00	Poorly sorted
6	Sorting	2.01 to 4.00	Very poorly sorted
7	Sorting	Greater than 4.00	Extremely poorly sorted
8	Skewness	Less than - 0.30	Very coarse skewed
9	Skewness	- 0.30 to - 0.11	Coarse skewed
10	Skewness	- 0.10 to +0.10	Near symmetrical
11	Skewness	+0.11 to +0.30	Fine skewed
12	Skewness	Greater than +0.30	Very fine skewed
13	Kurtosis	Less than 0.67	Very platykurtic
14	Kurtosis	0.67 to 0.90	Platykurtic
15	Kurtosis	0.91 to 1.11	Mesokurtic
16	Kurtosis	1.12 to 1.50	Leptokurtic
17	Kurtosis	1.51 to 3.00	Very leptokurtic
18	Kurtosis	Greater than 3.00	Extremely leptokurtic

**1.2 Coefficient of Variation (CV)**

This is also called Relative Standard Deviation (RSD) which is the standardized measure of dispersion of probability or frequency distribution. It is the ratio of the SD to the mean signifying the extent of variability in relation to the mean population. If CV is less than one, it is low variance; if it is greater than one, it is high variance. It is mostly expressed in percentage (Atat et al., 2022).

### 1.3 Geology of the Area of Study

In the Niger Delta, **A<sub>xx</sub>** Field is located, South of Port Harcourt, Rivers State, Nigeria. Niger Delta basin (Figure 1) is about latitudes 3°N to 6°N; longitudes 5°E to 8°E (Atat et al., 2020b; Akpabio et al., 2023a; Klett et al., 1997; Atat et al 2022; Akpabio et al., 2023b; Umoren et al., 2019). This region experiences wet and dry moments depending on the season in a year and the average rain in a month during wet season is about  $1.35 \times 10^2$ mm and reduces to  $6.50 \times 10^1$ mm while approaching dry season (Atat et al., 2020c; Atat et al., 2020d; George *et al.*, 2017; Atat and Umoren, 2016). The volume of sediment is nearly 500000km<sup>3</sup>. The oil in the basin belongs to the category of Akata-Agbada. More of marine shales made up the Akata formation with an expected width of up to  $7.0 \times 10^3$ m. The Agbada formation is the major oil reservoir in the Niger Delta (Atat et al., 2020c; Umoren et al., 2020; Udo *et al.*, 2017; Atat et al., 2020e; Hospers, 1965).

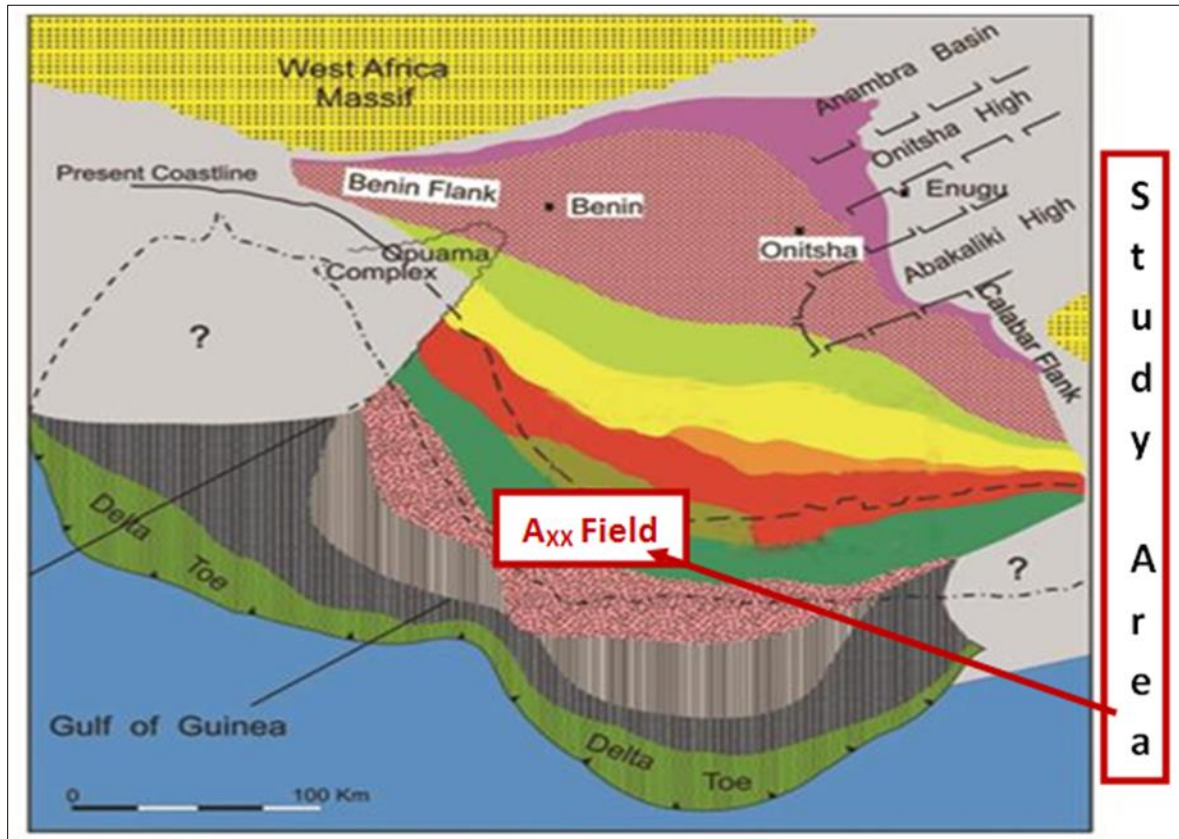


Figure 1 Map Showing the studied location

## 2 Materials and method

### 2.1 Material

Onshore **A<sub>xx</sub>** Field data was acquired from the Niger Delta Basin. These include well location and raw well data. (Depth, Gamma ray, Sonic and Density). With Microsoft Excel, data loading, processing, plots/curves, diagrams and other computations were accomplished.

### 2.2 Method

Three wells (A<sub>11</sub>, A<sub>22</sub> and A<sub>33</sub>) were studied. Suites of log such as depth, gamma ray, density and sonic were generated from the available data. These data were analyzed using Microsoft Excel. Figure 2 summaries the steps taken to attain at the goal.

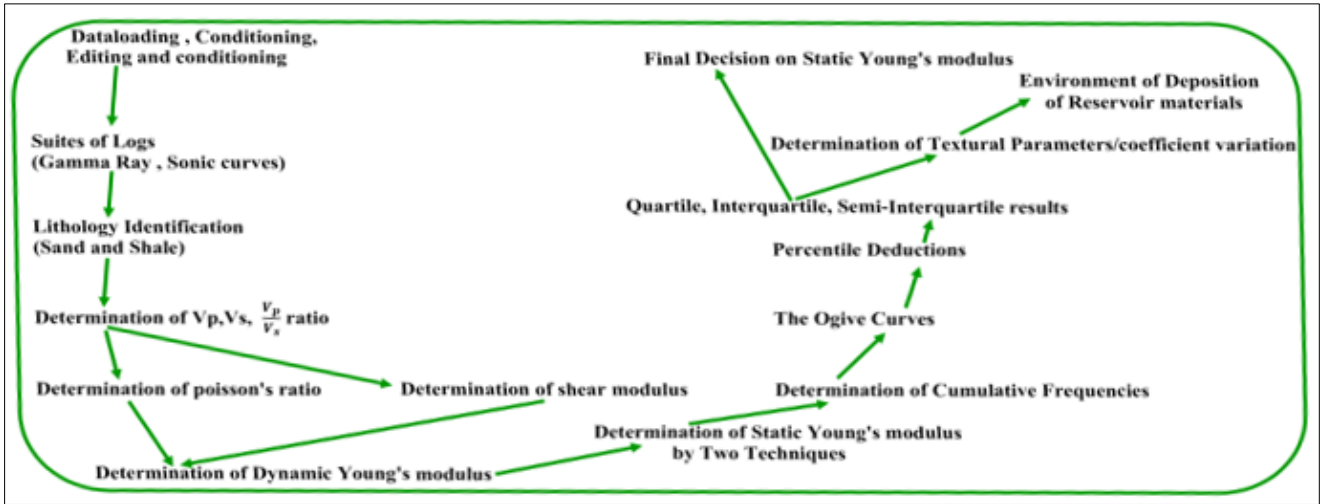


Figure 2 Workflow showing the analysis

### 3 Result

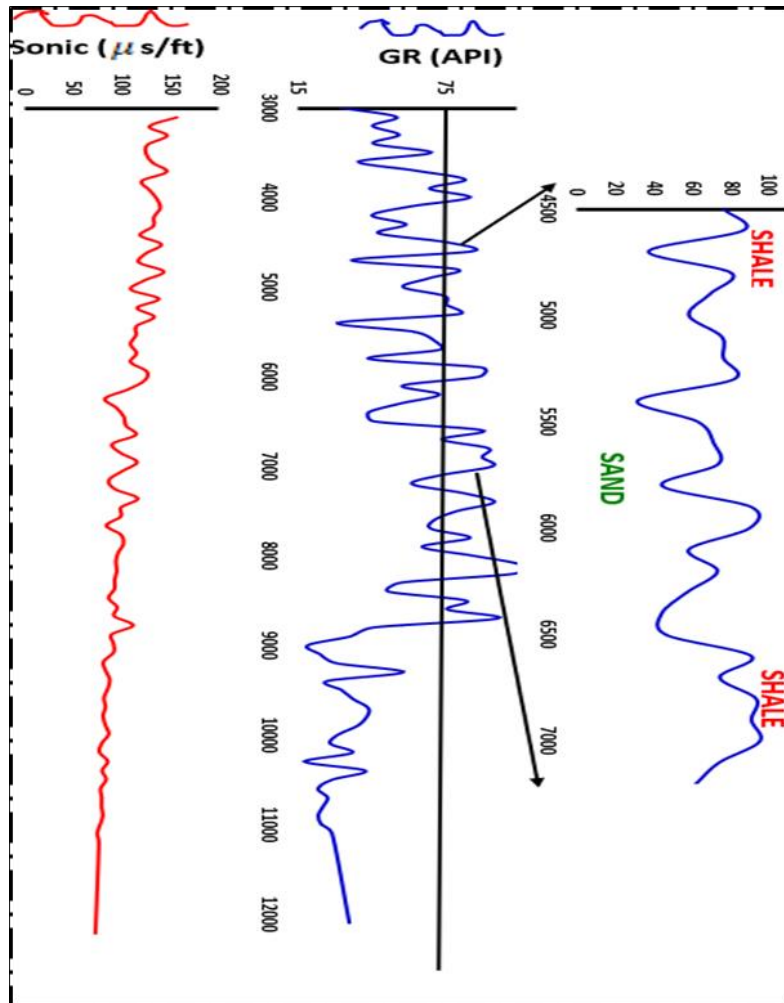
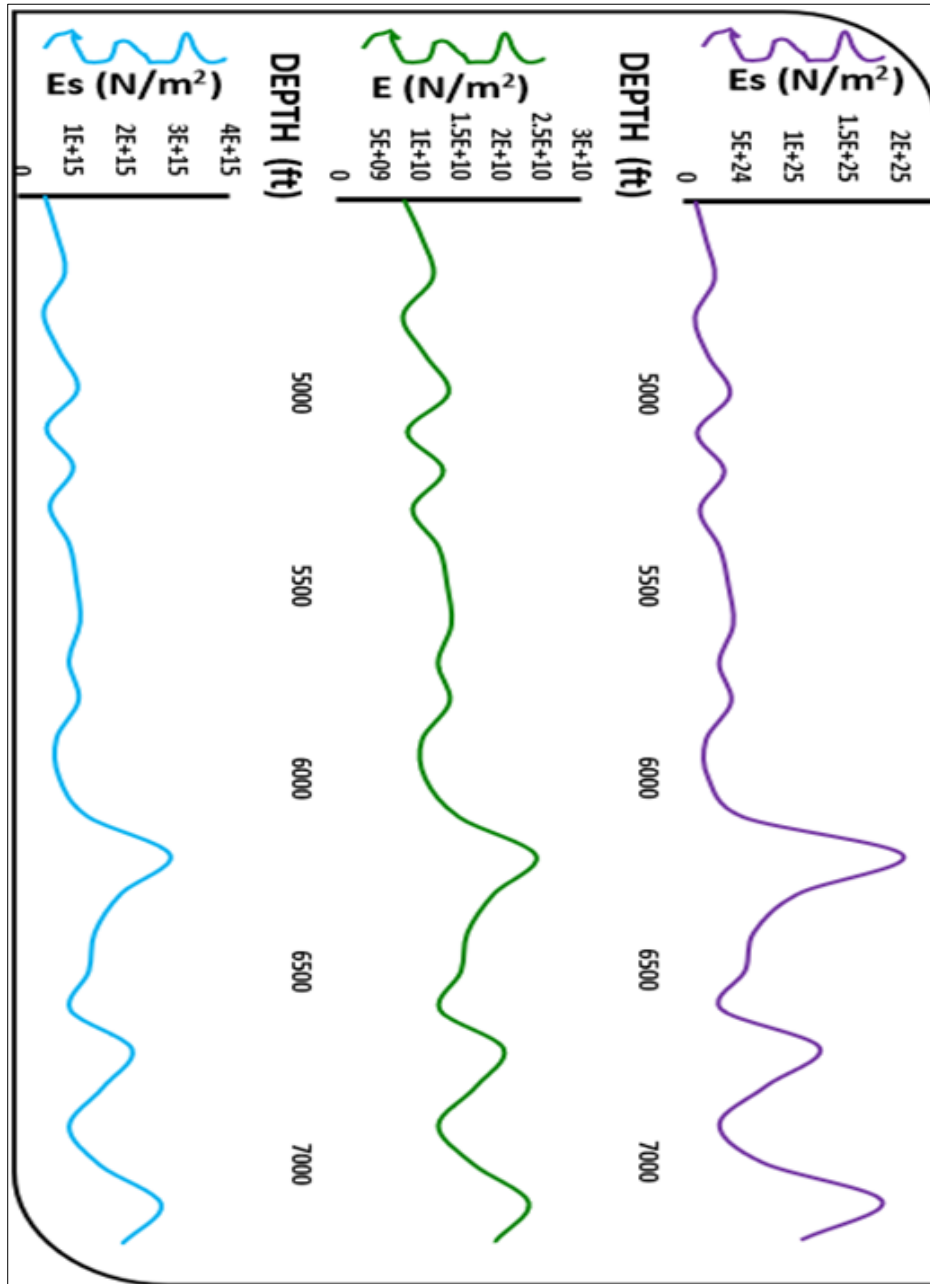


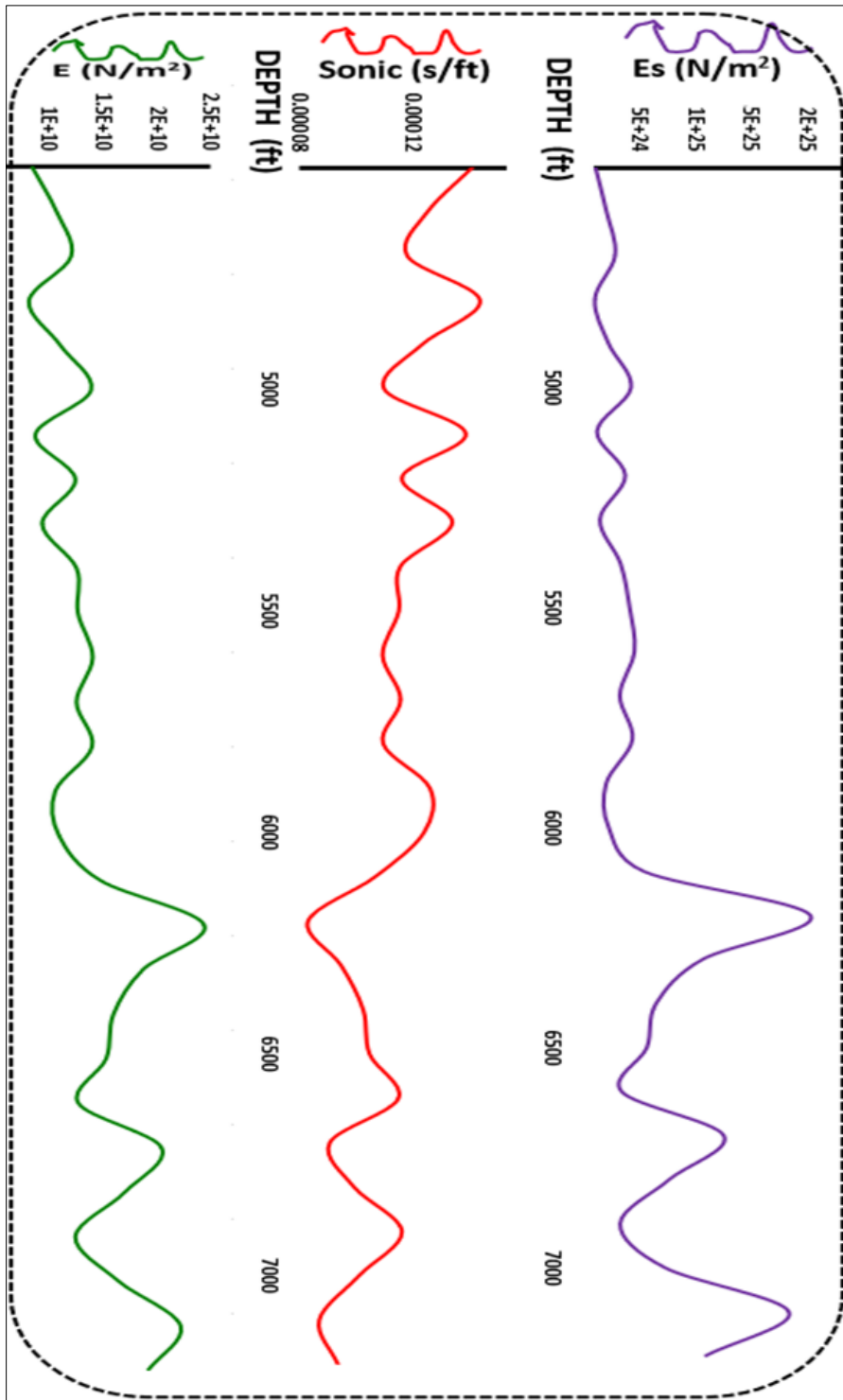
Figure 3 The generated suites of log with depth for gamma (blue) and sonic (red) indicating the sand/shale base line of Well A<sub>11</sub>

This research was conducted to determine the young’s modulus and define the reservoir materials in A<sub>xx</sub> field. These well data were obtained and generated into suites of log indicating the sand/shale baseline as presented in Figures 3, 6 and 9 for wells A<sub>11</sub>, A<sub>22</sub>, and A<sub>33</sub> respectively. Parameters (dependent variables) like compressional wave velocity, shear wave velocity, the ratio of these velocities was accounted for and shear modulus was determined. With the dependent variable information, Dynamic and Static young’s moduli were obtained (Figures 4, 7 and 10). Figures 5, 8 and 11 highlight the variation of the result of static young’s modulus with generated sonic curves. Figures 12, 13 and 14 became necessary in order to decide on a better static young’s modulus result. Table 2 shows the result of the percentiles obtained from the two techniques employed. Table 3 indicates the textural attributes and interpretation of the formation.



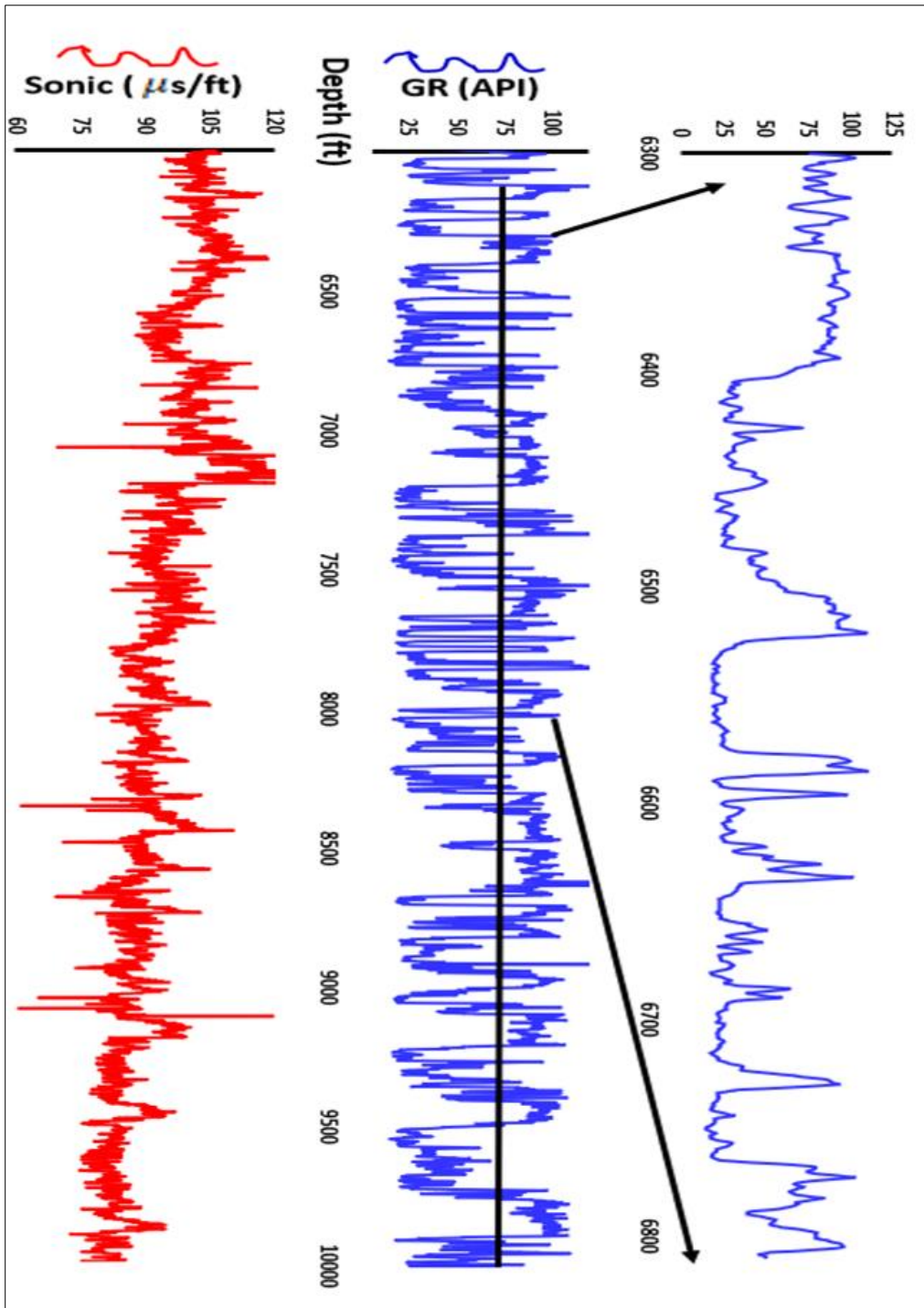
**Figure 4** Young’s modulus with depth curves (sky blue for static by AQ, green for dynamic and purple for static by AP) of well A<sub>11</sub>



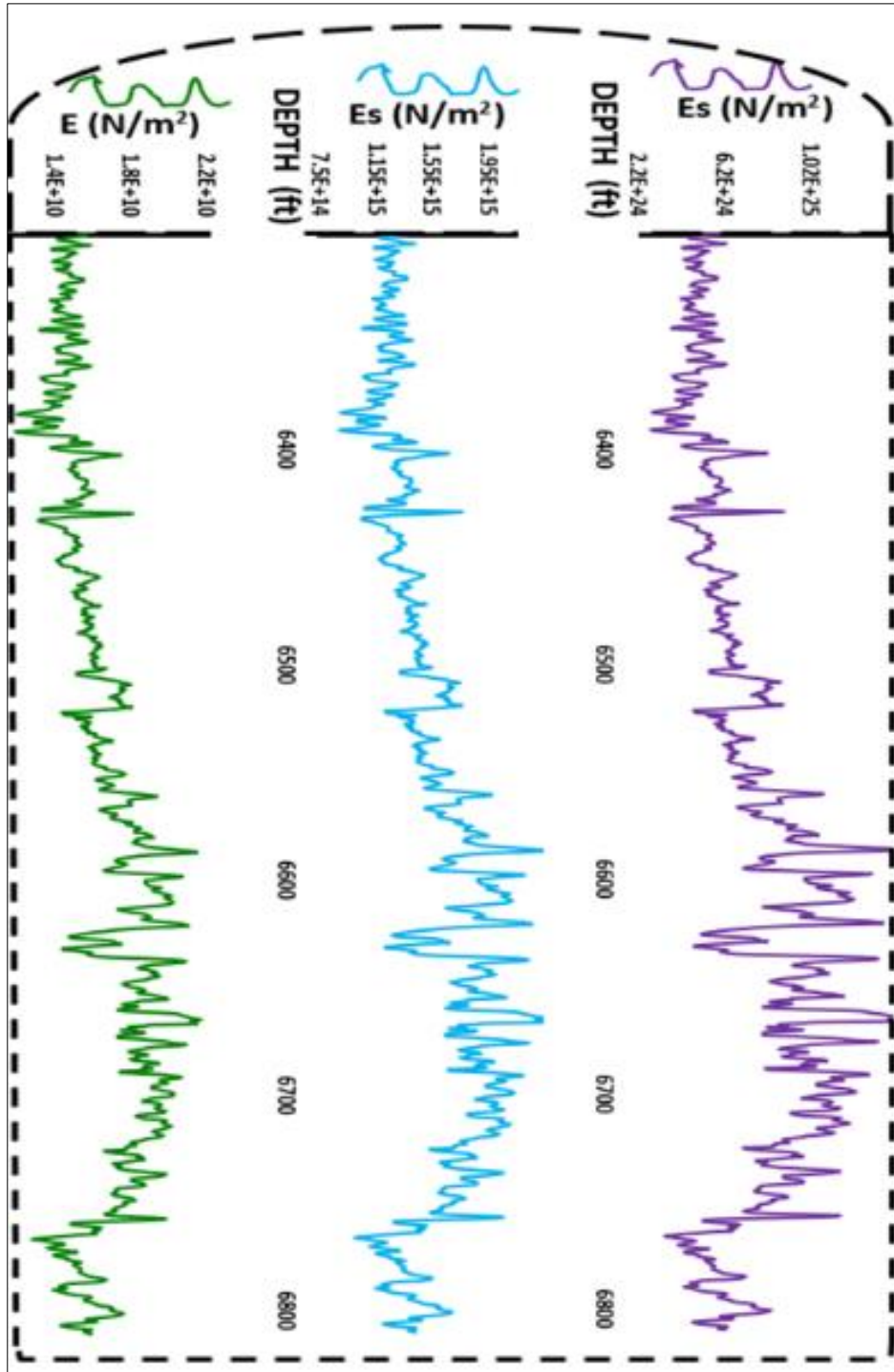


**Figure 5** The relationship between young's moduli (green for dynamic and purple for static), sonic (red) and depth from well A<sub>11</sub>

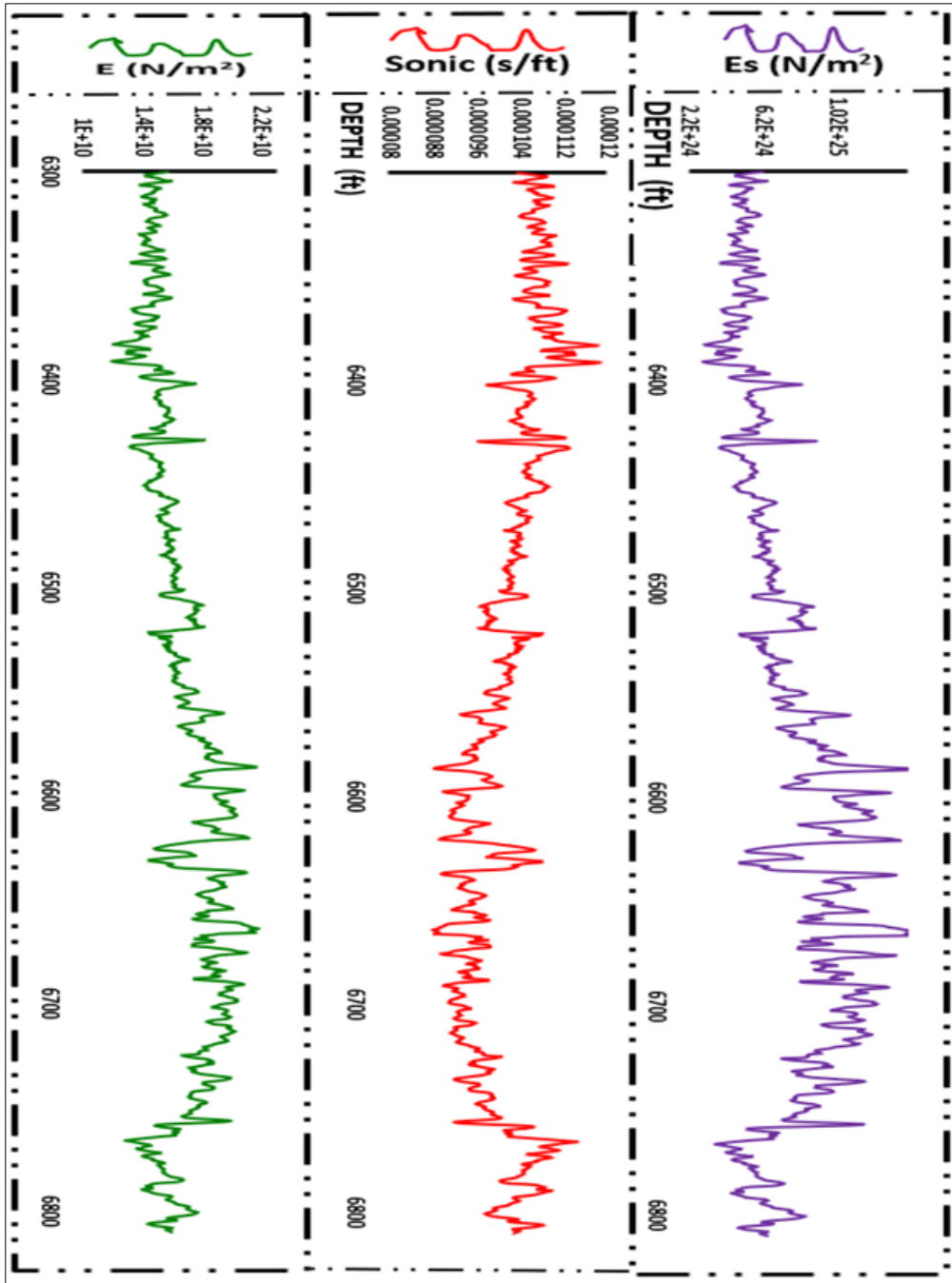




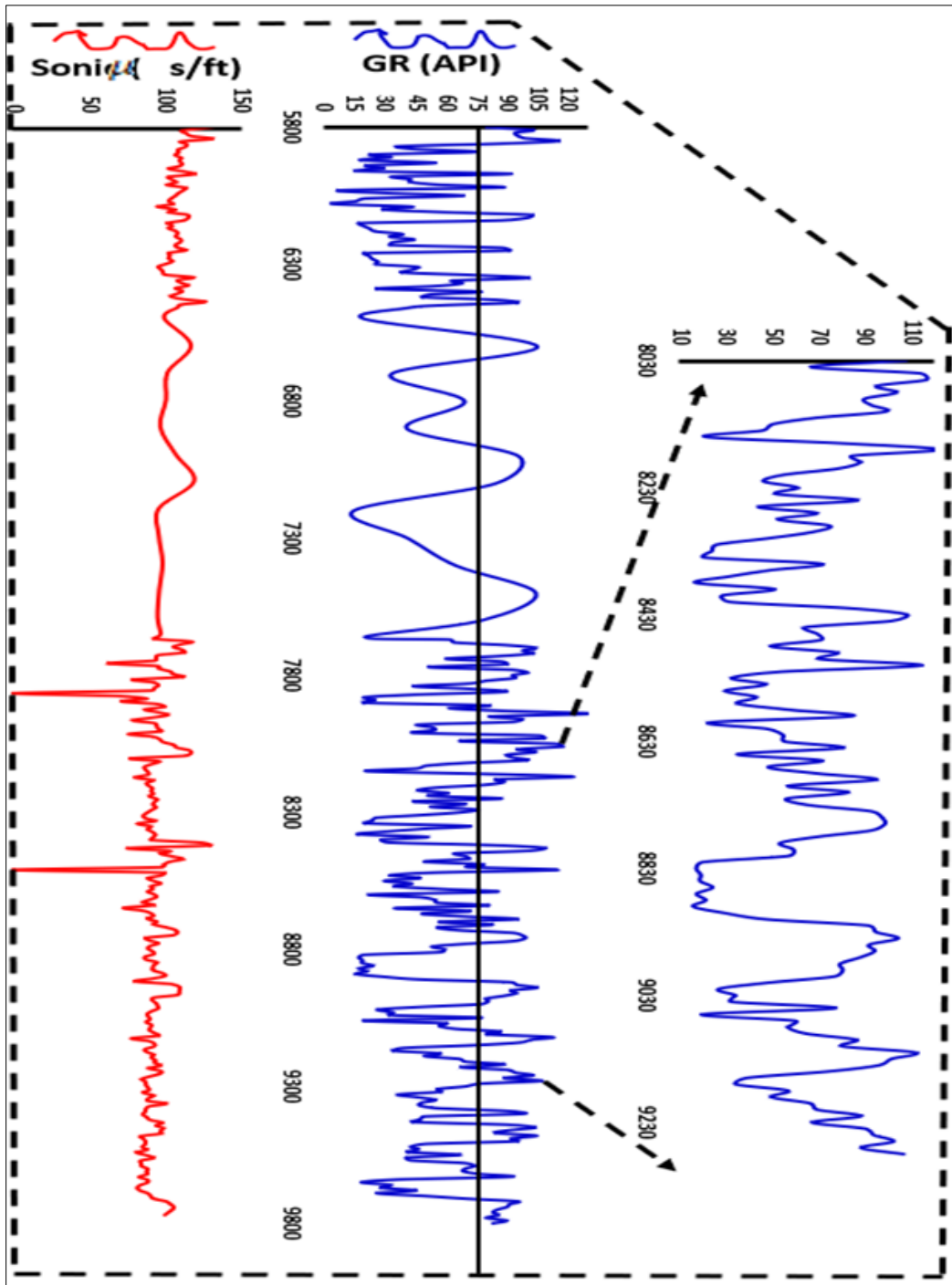
**Figure 6** The generated suites of log with for gamma (blue) and sonic (red) indicating the sand/shale base line of Well A<sub>22</sub>



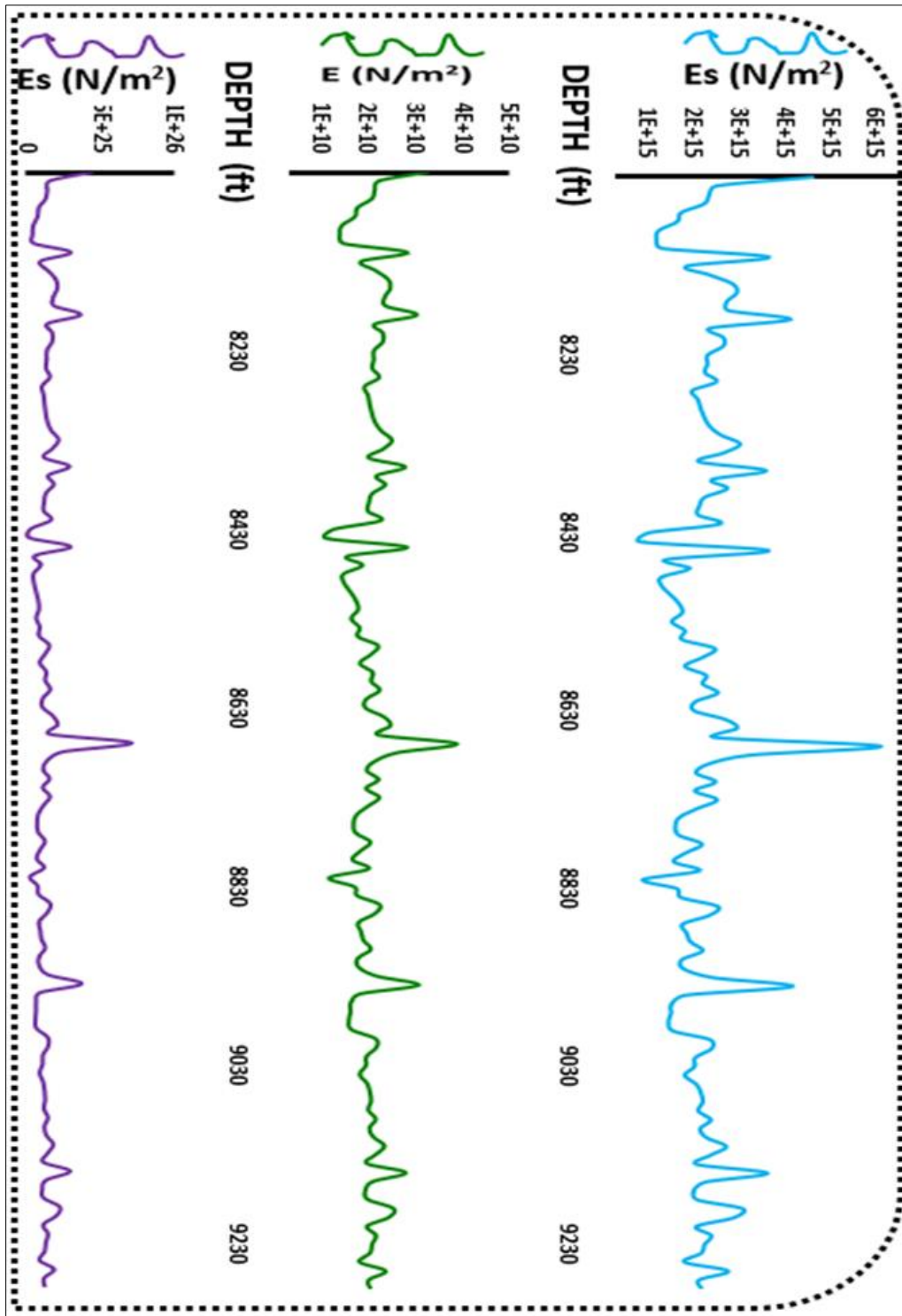
**Figure 7** Young's modulus with depth curves (sky blue for static by AQ, green for dynamic and purple for static by AP) of well A<sub>22</sub>



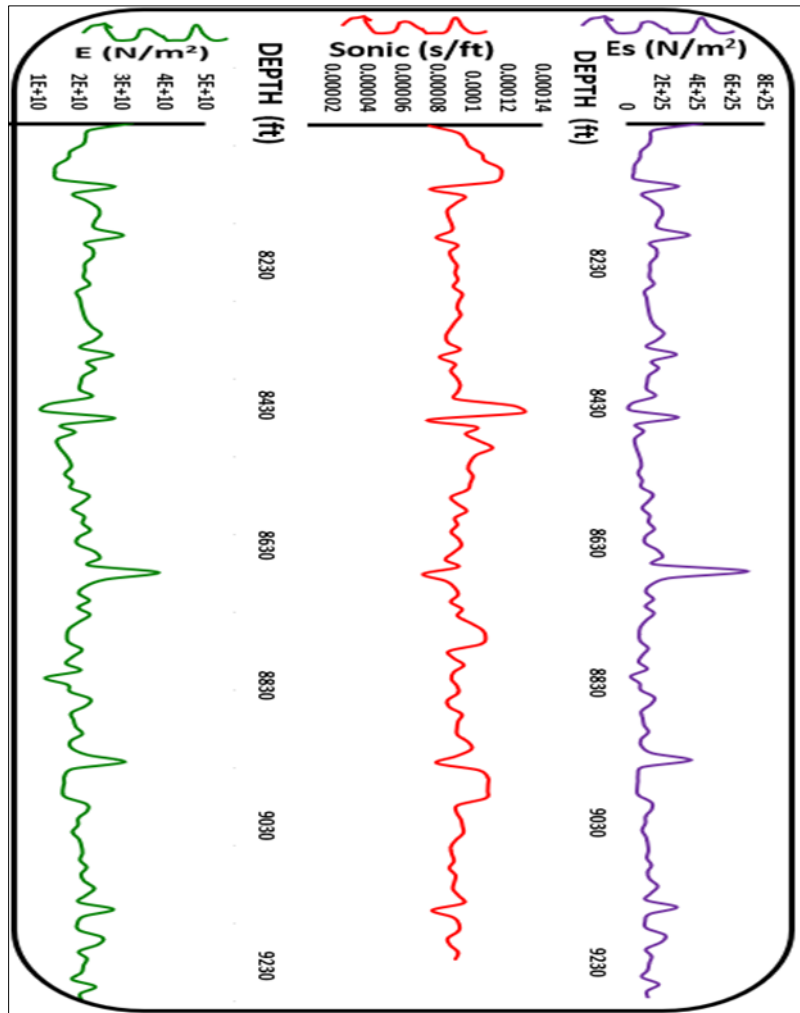
**Figure 8** The relationship between young's moduli (green for dynamic and purple for static), sonic (red) and depth from well A22



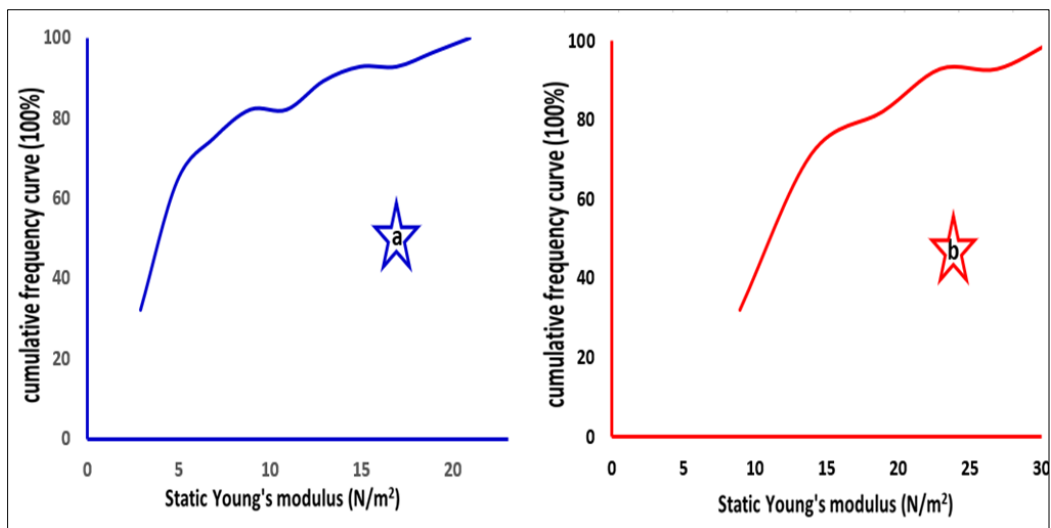
**Figure 9** The generated suites of log with depth for gamma (blue) and sonic (red) indicating the sand/shale base line of Well A33



**Figure 10** Young's modulus with depth curves (sky blue for static by AQ, green for dynamic and purple for static by AP) of well A33



**Figure 11** The relationship between young's moduli (green for dynamic and purple for static), sonic (red) and depth from well A33



**Figure 12** The Ogive resulting from Bradford technique (a) and Fuller technique (b) of Well A11.



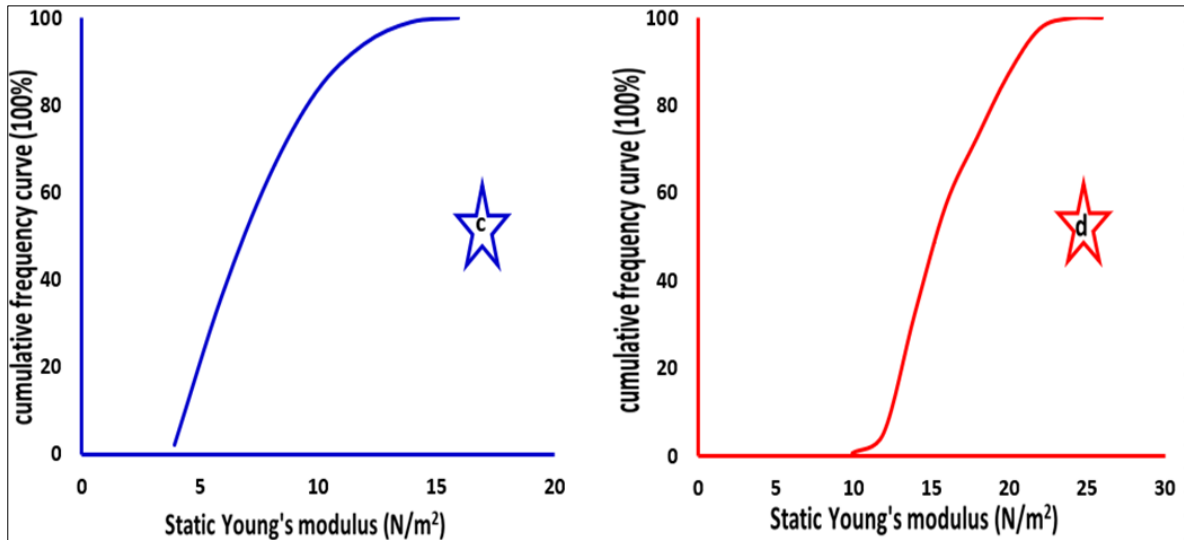


Figure 13 The Ogive resulting from Bradford technique (c) and Fuller technique (d) of Well A<sub>22</sub>

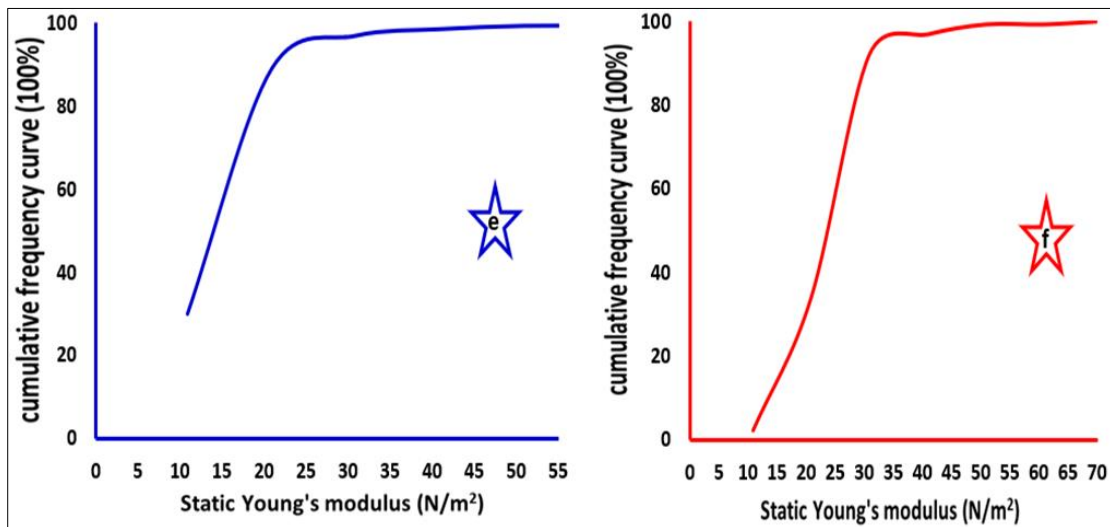


Figure 14 The Ogive resulting from Bradford technique (e) and Fuller technique (f) of Well A<sub>33</sub>

Table 2 The Percentiles obtained from each Technique and other Statistical Results

Wells	Techniques	Percentiles							SD	Mean	CV
		$\phi_5$	$\phi_{16}$	$\phi_{25}$	$\phi_{50}$	$\phi_{75}$	$\phi_{84}$	$\phi_{95}$			
A <sub>11</sub>	Bradford	1.5	2.1	2.6	4.0	6.9	11.5	18.2	2.35	5.86666667	0.4006
	Fuller	6.2	7.3	8.1	11.0	14.7	19.6	28.4	3.075	12.63333333	0.2434
A <sub>22</sub>	Bradford	4.1	4.7	5.2	6.8	9.0	10.0	12.2	1.325	7.16666670	0.1849
	Fuller	11.9	12.8	13.4	15.2	18.2	19.4	21.3	1.65	15.8000000	0.1044
A <sub>33</sub>	Bradford	7.0	8.2	10.0	12.0	18.0	19.0	25.0	2.7	13.06666667	0.2066
	Fuller	11.0	15.0	18.2	23.0	27.0	29.0	32.0	3.5	22.33333333	0.1567



**Table 3** The result of textural attributes and interpretation

Wells	Techniques	Sorting	skewness	Kurtosis	Interpretation
A <sub>11</sub>	Bradford	4.8803	0.64817	1.591689	Extremely poorly sorted, very fine skewed, very leptokurtic
A <sub>11</sub>	Fuller	6.43864	0.48297	1.378539	Extremely poorly sorted, very fine skewed, leptokurtic
A <sub>22</sub>	Bradford	2.55227	0.27044	0.873598	very poorly sorted, fine skewed, platykurtic
A <sub>22</sub>	Fuller	3.07424	0.2853	0.802596	very poorly sorted, fine skewed, platykurtic
A <sub>33</sub>	Bradford	5.42727	0.37037	0.922131	Extremely poorly sorted, very fine skewed, mesokurtic
A <sub>33</sub>	Fuller	6.68182	-0.1429	0.978018	Extremely poorly sorted, coarse skewed, mesokurtic

**Table 4** The Interquartile Range and Semi-Interquartile Range result summary

	Well A <sub>11</sub>		Well A <sub>22</sub>		Well A <sub>33</sub>	
Techniques	Bradford	Fuller	Bradford	Fuller	Bradford	Fuller
IQR	4.30	6.6	3.8	4.8	8.0	8.8
SIQR	2.15	3.3	1.9	2.4	4.0	4.4
Diff. M from Q <sub>3</sub>	2.90	3.7	2.2	3.0	6.0	4.0
Diff. M from Q <sub>1</sub>	1.40	2.9	1.6	1.8	2.0	4.8

## 4 Discussion

The data were loaded in Excel; spurious values were removed and suites of log generated for the three wells, with red colour signifying sonic and blue for Gamma ray (Figures 3, 6 and 9). The sand lithology and shale lithology were identified and marked as sand and shale where the Gamma ray index is about less than 75 API and greater than 75 API respectively. This thickness was considered and yielded more results about the reservoir, leading to young's modulus information.

Compressional wave velocity was determined from the sonic data. Shear wave velocity was determined using Castagna equation.  $\frac{V_P}{V_S}$  ratio is a value Poisson's ratio depends on, so it was determined as well as Poisson's ratio (Equation 3 was adequate). Shear modulus was determined using Equation 4. The calculation of dynamic young's modulus was done with Equation 2. Two static young's moduli results were obtained using two approaches (Bradford and Fuller techniques). In order to settle for the most accurate results, percentile deductions of quartile and interquartile information were necessary. The cumulative frequencies were determined and ogive plotted (Figure 12 to 14) correspondingly for wells A<sub>11</sub>, A<sub>22</sub>, and A<sub>33</sub>). Table 2 was computed from the ogive curves. The standard deviation and mean in Table 2 were calculated using Equations 7 and 6 respectively. Sorting, skewness and kurtosis were computed with Equations 8, 9 and 10 respectively. Table 1 was used for the interpretation.

### 4.1 For well A<sub>11</sub>,

The sand/shale investigated has a thickness of 2700ft (about 823m) which is from 4500ft to 7200ft. Red curve is for sonic, blue curve is for Gamma ray. The highest value of static young's modulus ( $2.048 \times 10^{25} \text{ N/m}^2$ ) is noted at 6200ft indicating that it does not depend on the depth of the reservoir. The lowest value ( $1.05 \times 10^{24} \text{ N/m}^2$ ) is noted at 4800ft. For dynamic young's modulus, its highest value is ( $1.93 \times 10^{10} \text{ N/m}^2$ ) at 6200ft and lowest value is ( $8.5 \times 10^9 \text{ N/m}^2$ ) at 4800ft. Therefore, increase in dynamic young's modulus leads to an increase in static young's modulus. This finding agrees with Figure 4. The sky blue is the static young's modulus from Fuller technique, green is dynamic young's modulus and purple represents static young's modulus from Bradford approach. Relating the final result of young's moduli with sonic log shows that increase in sonic information leads to a decrease in young's modulus. The choice of the most accurate result of static young's modulus was from the percentile deductions which involved Figure 12 and Table 2. Table 2 presents the values of IQR and SIQR obtained from Bradford approach as lower than those computed from Fuller technique. Moreso, Fuller values deviate strongly from the median than Bradford values. Table 3 defines the

reservoir environment as extremely poorly sorted, very fine skewed and very leptokurtic. With this information, it is a low energy environment. According to Britt and Schoeffler (2009), static young's modulus greater than  $3.5 \times 10^6$  psi (which is about 20.684Gpa) will be brittle as one of the important elastic properties of rock. Since both the lowest and highest values of the static young's modulus obtained in this research is greater than this standard, therefore the reservoir rock is brittle. Brittleness refers to the ability of a material to fracture or break under stress without significant deformation. It is often used to characterize the mechanical behavior of rocks.

#### 4.2 For well A<sub>22</sub>,

The sand/shale investigated has a thickness of 510ft (156m) which is from 6300ft to 6810ft. Red curve is for sonic, blue curve is for Gamma ray. The highest value of static young's modulus ( $1.47 \times 10^{25}$ N/m<sup>2</sup>) is noted at 6664ft indicating that it does not depend on the depth of the reservoir. The lowest value ( $9.01315 \times 10^{14}$ N/m<sup>2</sup>) is noted at 6391ft. For dynamic young's modulus, its highest value is ( $1.5848 \times 10^{10}$ N/m<sup>2</sup>) at 6664ft and lowest value is ( $1.5726 \times 10^{10}$ N/m<sup>2</sup>) at 6391ft. Therefore, increase in dynamic young's modulus leads to an increase in static young's modulus. this finding agrees with Figure 7. The sky blue is the static young's modulus by Fuller technique, green is dynamic young's modulus and purple represents static young's modulus by Bradford approach. Relating the final result of young's moduli with sonic log shows that increase in sonic information leads to a decrease in young's modulus. The choice of the most accurate result of static young's modulus was from the percentile deductions which involved Figure 13 and Table 2; Table 2 values of IQR and SIQR obtained from Bradford approach are lower than those computed from Fuller technique. Moreso, Fuller values deviate strongly from the median than Bradford values. Table 3 defines the reservoir environment as very poorly sorted, fine skewed and platykurtic. With this information, it is a low energy environment. Britt and Schoeffler (2009), stated that static young's modulus greater than  $3.5 \times 10^6$  psi (which is about 20.684Gpa) will be brittle as one of the important elastic properties of rock. Since both the lowest and highest values of the static young's modulus obtained in this research are greater than this standard, the reservoir rock is brittle. Brittleness refers to the ability of a material to fracture or break under stress without significant deformation. It is often used to characterize the mechanical behavior of rocks. Brittle materials are solid materials that tend to fracture or break under stress without significant deformation.

#### 4.3 For well A<sub>33</sub>

The sand/shale investigated has a thickness of 1250ft (about 381m) which is from 8030ft to 9280ft. Red curve is for sonic, blue curve is for Gamma ray. The highest value of static young's modulus ( $7.08 \times 10^{25}$  N/m<sup>2</sup>) is noted at 8670ft indicating that it does not depend on the depth of the reservoir. The lowest value ( $8.36 \times 10^{14}$ N/m<sup>2</sup>) is noted at 8440ft. For dynamic young's modulus, its highest value is ( $2.04 \times 10^{10}$ N/m<sup>2</sup>) at 8670ft and lowest value is ( $3.28 \times 10^{10}$ N/m<sup>2</sup>) at 8440ft. Therefore, increase in dynamic young's modulus leads to an increase in static young's modulus. this finding agrees with Figure 10. The sky blue is the static young's modulus by Fuller technique, green is dynamic young's modulus and purple represents static young's modulus by Bradford approach. Linking the final result of young's moduli with sonic log shows that increase in sonic information leads to a decrease in young's modulus. the choice of the most accurate result of static young's modulus was from the percentile deductions which involved Figure 14 and Table 2. The values of IQR and SIQR (Table 2) obtained from Bradford approach are lower than those computed from Fuller technique. Moreso, Fuller values deviate strongly from the median than Bradford values. Table 3 defines the reservoir environment as extremely poorly sorted, very fine skewed and mesokurtic. Therefore, it is a low energy environment. Britt and Schoeffler (2009) findings indicated that static young's modulus greater than  $3.5 \times 10^6$  psi (which is about 20.684Gpa) will be brittle as one of the important elastic properties of rock. Since both the lowest and highest values of the static young's modulus obtained in this research is greater than this standard, therefore the reservoir rock is brittle. Brittleness refers to the ability of a material to fracture or break under stress without significant deformation. It is often used to characterize the mechanical behavior of rocks.

Young's modulus is typically used to characterize the stiffness of solid materials and their response to applied stress and strain. The Coefficient of Variation (CV) is low in both techniques but the choice of a better technique was derived from the deviation from the median.

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## 5 Conclusion

The young's modulus increases with a decrease in sonic. It is not influenced by the depth. Static young's modulus increases with increase in dynamic young's modulus. The result obtained classifies this elastic property as brittle. The wells would certainly stand a test of time without collapsed. The textural parameters defined the formation as brittle whose environment is extremely poorly sorted, very fine skewed and very leptokurtic with low energy for well A<sub>11</sub>, very poorly sorted, fine skewed and platykurtic for well A<sub>22</sub>, extremely poorly sorted, very fine skewed and mesokurtic for well A<sub>33</sub>.

## Compliance with ethical standards

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### *Disclosure of conflict of interest*

No conflict of interest to be disclosed.

### *Statement of ethical approval*

The Author confirms that the work described has not been published before; that it is not under consideration for publication elsewhere; that its publication has been approved by all co-authors; the copyright is transferred when the article is accepted for publication. The corresponding author signs for and accepts responsibility for releasing this material on behalf of any and all co-authors. The copyright transfer covers the exclusive right to reproduce and distribute the article.

### *Statement of Informed consent*

Informed consent was obtained from all individual participants included in the study. The Authors consent to participate in the research project and the outcome of our investigation result in this article. The participation of the Authors is completely voluntary and they have agreed to publish this finding in International Journal of Scientific Research Updates as a research article.

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