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(n+/p/p+) Silicon solar cell base thickness optimization under modulated short wavelength illumination, at resonances in both frequency and temperature of minority carriers' diffusion coefficient

Ousmane SOW^{1, 2}, Sega GUEYE¹, Richard MANE¹, Gora DIOP¹, Ibrahima DIATTA¹, Khady LOUM^{1, 2}, Moustapha THIAME^{1,3}, Mamadou WADE^{1,4} and Gregoire SISSOKO^{1,*}

¹ International Renewable Energy Research Group (GIRER). BP. 15003, Dakar, Senegal.

² University Institute of Technology. Iba Der THIAM University of Thiès-Senegal.

³ Assane SECK University, Ziguinchor, Senegal.

⁴ Polytechnic School of Thiès, BP A10, Thiès, Senegal.

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Abstract

The magneto-transport equation relating to the density of photogenerated minority carriers in the (p) base of the (n+/p/p+) solar cell illuminated by monochromatic light in frequency modulation, is solved. The diffusion coefficient of the minority carriers in the base, placed under temperature and magnetic field variation, passes through a maximum, at the double resonance points, in temperature and at the frequency of the cyclotron. The photocurrent is reproduced as a function of the recombination velocity at the junction, for the maximum values of the diffusion coefficient. The expressions of the minority carriers' recombination velocity on the rear side are deduced and their graphical representation gives the optimum thickness, specific to a high absorption coefficient, for the maximum values of the diffusion coefficient. The results obtained from the optimum thickness are modelled and analyzed, in favor of a reduction of silicon material, for the development of economical solar cells.

Keywords: Silicon Solar Cell; Diffusion Coefficient; Resonance-Temperature; Magnetic field; Recombination Velocity; Absorption coefficient; Optimum Base Thickness

1 Introduction

The search for solar cell efficiency improvement, led to the optimization of the thickness of the base [1, 2], by the characterization of samples with different thicknesses, cut from the massif [3, 4, 5, 6, 7]. However, the depth of the other regions (emitter and space charge region) of the solar cell are also important [8, 9, 10] and allow the decoupling of the physical mechanisms that govern the operation of the solar cell [11, 12].

This work consists in looking for the optimum thickness of the (p) base [1, 2, 13, 14, 15, 16, 17, 8, 19] of a silicon solar cell (n+/p/p+) [20, 21], when subjected to a magnetic field (B) and placed under a temperature (T).

It is then illuminated by a monochromatic light in frequency modulation (ω) [22, 23, 24, 25, 26], of short wavelength (λ), inducing a very large absorption coefficient ($\alpha(\lambda)$) of the material (Si) [27, 28].

* Corresponding author: Gregoire SISSOKO

International Renewable Energy Research Group (GIRER). BP. 15003, Dakar, Senegal.

The illumination then, penetrates weakly into the base [29] and therefore the carriers are photogenerated near the junction in the base, because $(\alpha(\lambda))$ is very large and they are subsequently subjected to Lorentz's law (effect of B) [30, 31, 32] and the Umklapp process due to thermal agitation (effect of T) [33, 34, 35, 36, 37, 35].

Under these conditions the diffusion coefficient $D(\omega, B, T)$ of the minority charge carriers in the base under the action of the variation of (B) undergo the ringing effect:

- At the cyclotron frequency (ω_c) [39, 40, 41]
- At the optimum temperature (T_{opt}) [35]
- This double resonances, in frequency and temperature makes it possible to establish a new expression of the diffusion coefficient $D(\omega_c, T_{opt})$ of the minority carriers in the base [42].

The diffusion equation of the minority carriers in the base is then solved and the solution $\delta(x, \omega, B, T, \alpha(\lambda))$ of the density of the minority charge carriers is completed by taking into account boundary conditions in the base, which are (Sf) and (Sb), respectively recombination rates [11, 43] at the junction (n+/p) [44, 45, 46, 47, 48] and back side (p/p+)[49, 50, 51, 52].

From the profile obtained, the density of the photocurrent $J_{ph}(D(\omega_c, T_{opt}), \alpha(\lambda), H, S_f, S_b)$ as a function of the recombination velocity (Sf), the expressions of the recombination velocity

$(S_b [D(\omega_c, T_{opt}), \alpha(\lambda), H])$ are established [53, 54, 55, 56, 57]. The representation of these expressions [1, 2, 13, 14, 15, 16, 17] in the form of bi-axis curves as a function of thickness (H), for different values of $D(\omega_c, T_{opt})$ and given $\alpha(\lambda)$, allow to extract the optimum thickness (H_{opt}) , which is then modeled as a function of both $D(\omega_c, T_{opt})$, and T_{opt} .

2 Theory

The front illuminated (n+-p-p+) silicon solar cell [20, 21] with modulated monochromatic light, and placed under magnetic field B and temperature T, is presented below, by figure 1

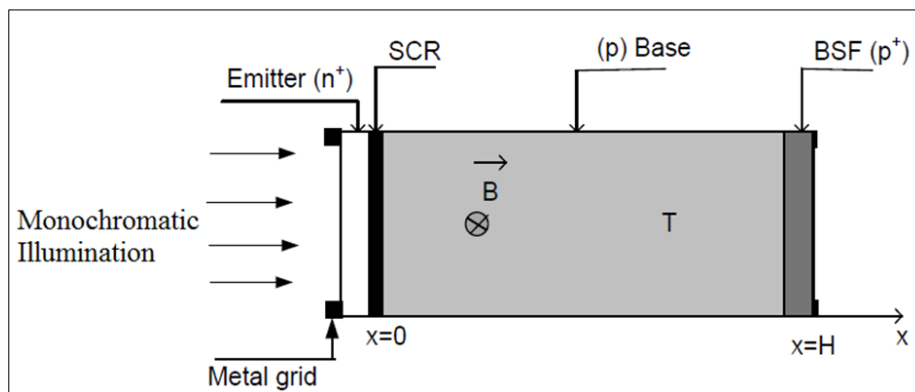


Figure 1 Structure of front illuminated solar cell

The excess minority carriers' density $\delta(x, t)$ generated in the base of the solar cell obeying to the magneto-transport equation at T temperature, under monochromatic illumination in frequency modulation, is given by [5, 6, 25, 58]:

$$D(\omega, B, T) \times \frac{\partial^2 \delta(x, t)}{\partial x^2} - \frac{\delta(x, t)}{\tau} = -G(x, \omega, t) + \frac{\partial \delta(x, t)}{\partial t} \dots\dots\dots(1)$$

The expression of the excess minority carriers' density is written, according to the space coordinates (x) and the time t, as:

$$\delta(x, t) = \delta(x) \cdot e^{-j\omega t} \dots\dots\dots(2)$$

The excess minority carriers' lifetime in the base is (τ) and the generation rate $G(x, t)$ is given by the following relationship:

$$G(x, t) = g(x) \cdot e^{-j\omega t} \dots\dots\dots (3)$$

With:

$$g(x) = \alpha(\lambda) \cdot I_0(\lambda) \cdot (1 - R(\lambda)) \cdot e^{-\alpha(\lambda) \cdot x} \dots\dots\dots (4)$$

$I_0(\lambda)$ is the monochromatic incident flux, while $\alpha(\lambda)$ and $R(\lambda)$ are optical parameters of Si material [27, 28, 59, 60, 61].

$D(\omega, B, T)$ is the complex diffusion coefficient of excess minority carrier in the base under magnetic field and temperature and frequency modulation [39, 40]. The solution of equation (1) is:

$$\delta(x, \omega, B, T) = A \cdot \cosh\left[\frac{x}{L(\omega, B, T)}\right] + E \cdot \sinh\left[\frac{x}{L(\omega, B, T)}\right] + K \cdot e^{-\alpha \cdot x} \dots\dots\dots (5)$$

With

$$K = \frac{\alpha \cdot I_0 \cdot (1 - R) \cdot [L(\omega, B, T)]^2}{D(\omega, B, T) [L(\omega, B, T)^2 \cdot \alpha^2 - 1]} \dots\dots\dots (6)$$

And

$$(L(\omega, B, T)^2 \cdot \alpha^2 \neq 1) \dots\dots\dots (7)$$

Coefficients A and E are determined through the boundary conditions expressed as:

At the junction ($x = 0$)

$$\left. \frac{\partial \delta(x, \omega, B, T)}{\partial x} \right|_{x=0} = S_f \cdot \left. \frac{\delta(x, \omega, B, T)}{D(\omega, B, T)} \right|_{x=0} \dots\dots\dots (8)$$

On the back side in the base ($x = H$)

$$\left. \frac{\partial \delta(x, \omega, B, T)}{\partial x} \right|_{x=H} = -S_b \cdot \left. \frac{\delta(x, \omega, B, T)}{D(\omega, B, T)} \right|_{x=H} \dots\dots\dots (9)$$

The excess minority carriers' recombination velocities are S_f and S_b respectively at the junction [44, 45, 47] and at the back surface [44, 49, 50].

3 Results

3.1 Minority carriers' diffusion Coefficient

- Its expression is given by the relationship [39, 40]:

$$D(\omega, B, T) = D(B, T) \times \frac{\left[\left(1 + \tau^2 (\omega_c(B)^2 + \omega^2) \right) + j\omega\tau \left[\tau^2 (\omega_c(B)^2 - \omega^2) - 1 \right] \right]}{\left[1 + \tau^2 (\omega_c(B)^2 - \omega^2) \right]^2 + 4\omega^2\tau^2} \dots\dots\dots (10)$$

With the cyclotron frequency expressed as :

$$\omega_c = \frac{q \cdot B}{m_e^*} \dots\dots\dots (11)$$

$D(B, T)$ is the diffusion coefficient of the excess minority carriers in the base of the solar cell, under magnetic field and under temperature.

Under magnetic field, the diffusion coefficient is given by the following relation [30, 32]:

$$D(B, T) = \frac{D(T)}{1 + (\mu B)^2} \dots\dots\dots (12)$$

With :

$$D(T) = \frac{\mu(T) \cdot K \cdot T}{q} \dots\dots\dots (13)$$

And the mobility coefficient is given as [5, 38]:

$$\mu(T) = 1,43 \cdot 10^{19} \cdot T^{-2,42} \dots\dots\dots (14)$$

The representation of the diffusion coefficient of the minority charge carriers as a function of temperature admits a maximum corresponding to the optimum temperature $T_{opt}(\omega, B)$. The optimum temperature is obtained by solving the following equation [42]:

$$\frac{dD(\omega, B, T)}{dT} = 0 \dots\dots\dots (15)$$

From this equation one can deduce the values of the optimum temperature $T_{opt}(\omega, B)$ for different values of the cyclotron frequency and magnetic field (**Table.1**). Finally we get [42]:

$$T_{opt}(\omega, B) = \sqrt[{-1,84}]{\frac{2,272 \times 10^{-19}}{1,184 \times B^2} \frac{\left[\left(1 + \tau^2 (\omega_c(B)^2 + \omega^2) \right) + j\omega\tau \left[\tau^2 (\omega_c(B)^2 - \omega^2) - 1 \right] \right]}{j\omega\tau^3 \omega_c(B)^2 - j\omega^3\tau^3 - j\omega\tau + \left[1 + \tau^2 (\omega_c(B)^2 + \omega^2) \right]}} \dots\dots\dots (16)$$

Table 1 Maximum values of minority carriers’diffusion coefficient and optimal temperature for different cyclotron frequency and magnetic field values

ω_c (B) rad/s	5,30.10⁷	7,03.10⁷	8,84.10⁷	1,06.10⁸	1,76.10⁸
B(Tesla)	3.10 ⁻⁴	4.10 ⁻⁴	5.10 ⁻⁴	6.10 ⁻⁴	10 ⁻³
D (cm ² /s)	16,212	14,079	11,138	9,934	8,108
T _{opt} (K)	257	290	318	343	424

3.2 Photocurrent

The photocurrent density at the junction is deduced from the density of minority carriers in the base and is expressed as:

$$J_{ph}(Sf, Sb, \omega, B, T) = qD(\omega, B, T) \left. \frac{\partial \delta(x, Sf, Sb, \omega, B, T)}{\partial x} \right|_{x=0} \dots\dots\dots (17)$$

Where q is the elementary electron charge.

Figure 2 shows, ac photocurrent versus junction surface recombination velocity for different diffusion coefficient values (Dmax).

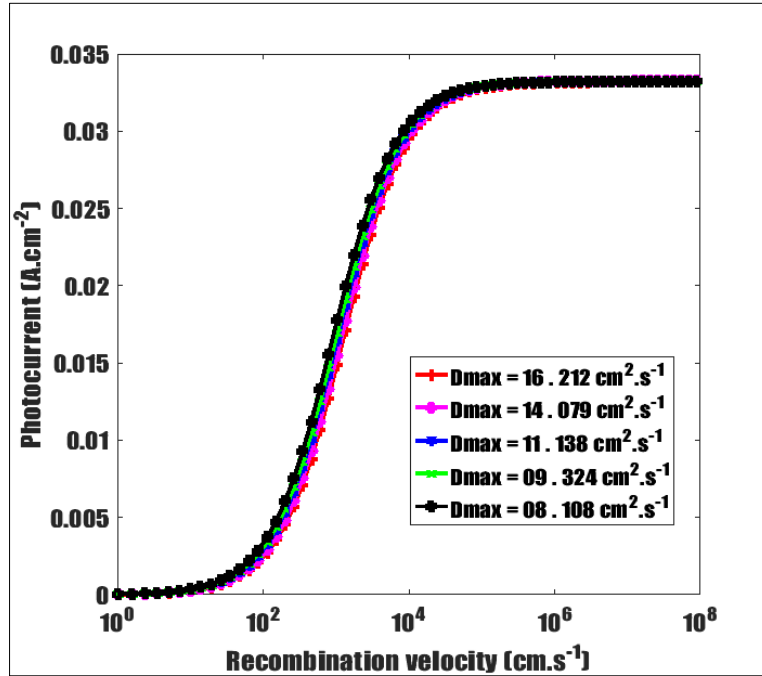


Figure 2 Module of photocurrent density versus recombination velocity for different diffusion coefficient ($\alpha = 21000 \text{ cm}^{-1}$)

Figure 2 shows the photocurrent density obtained with strong absorption coefficient versus the junction surface recombination velocity for different diffusion coefficient (Dmax).

On figure.2, for large (Sf) values, variation in the short circuit current with Dmax is small). Indeed the monochromatic light of short wavelength corresponding to a large ($\alpha(\lambda)$) value, penetrates weakly into the solar cell. Then charge carriers are photogenerated near the junction. The distance to reach the junction is short, hence the deflection induced by (B) has very weak impact. The deflection phenomenon can be underestimated, compare to the effect of high monochromatic absorption coefficient ($\alpha(\lambda)$) value.

The increase in the modulation frequency (ω) brings the maximum density of the charge carriers closer to the junction [2, 13, 19, 54]. Then the photocurrent represented in the figure. 2, is not very sensitive to the effect of deflection due to the magnetic field (B). The effect of large frequencies is analogous to that of large monochromatic absorption coefficient ($\alpha(\lambda)$) value [2, 13, 17, 18, 19, 29, 41, 54].

3.3 Base thickness optimization

For very large Sf, the representation of photocurrent density according to the junction recombination velocity of minority carriers shows the short-circuit current density (Jphsc), that is constant whatever the diffusion coefficient (Dmax). So, in this velocity interval of junction recombination, we can write [44, 48, 50, 51, 52, 53, 54, 57]:

$$\left. \frac{\partial J_{ph}(Sf, Sb, \alpha, \omega, B, T)}{\partial Sf} \right|_{Sf \geq 10^5 \text{ cm.s}^{-1}} = 0 \dots\dots\dots (18)$$

The solution of equation (18) leads to the ac recombination velocity in the back surface expressions given by equations (19) and (20):

$$Sb1(\omega, B, T) = -\frac{D(\omega, B, T)}{L(\omega, B, T)} \cdot \tanh\left(\frac{H}{L(\omega, B, T)}\right) \dots\dots\dots (19)$$

$$Sb2(\omega, B, T, \lambda) = \frac{D(\omega, B, T)}{L(\omega, B, T)} \cdot \left[\frac{\alpha(\lambda) \cdot L(\omega, B, T) \cdot \left(\exp(-\alpha(\lambda) \cdot H) - \cosh\left(\frac{H}{L(\omega, B, T)}\right) + \sinh\left(\frac{H}{L(\omega, B, T)}\right) \right)}{\exp(-\alpha(\lambda) \cdot H) - \cosh\left(\frac{H}{L(\omega, B, T)}\right) + \alpha(\lambda) \cdot L(B, T) \cdot \sinh\left(\frac{H}{L(\omega, B, T)}\right)} \right] \dots\dots\dots (20)$$

The figure 3 gives back surface recombination velocity representation versus solar cell base thickness as described in previous works [1, 2, 13, 14,15, 16, 17, 18, 19, 62, 63, 64]., for different maximum diffusion coefficient in our case.

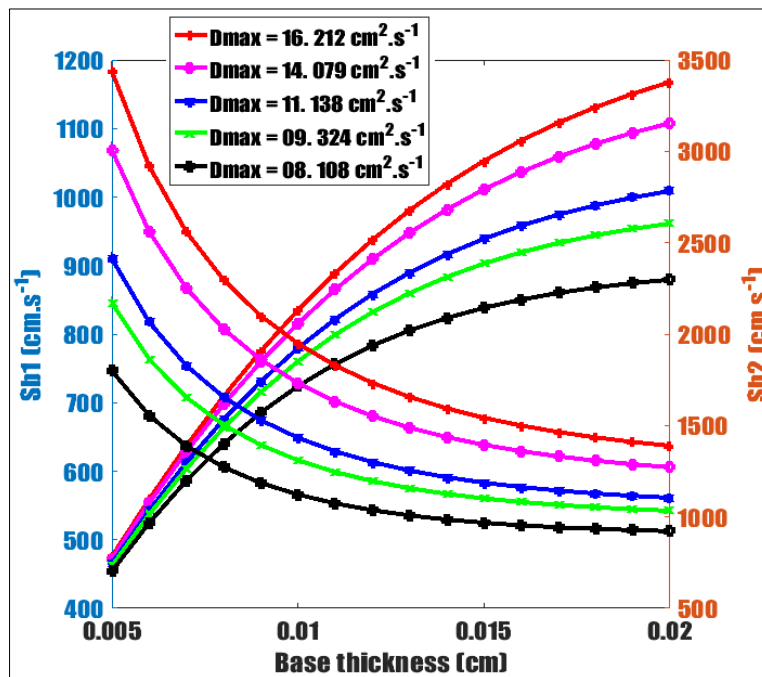


Figure 3 Sb1 and Sb2 versus depth in the base for different diffusion coefficient

Table 2 Base optimum thickness obtained with maximum values of minority carriers' diffusion coefficient and optimal temperature for different cyclotron frequency and magnetic field values

$\omega_c (B)$ rad/s	$5.30 \cdot 10^7$	$7.03 \cdot 10^7$	$8.84 \cdot 10^7$	$1.06 \cdot 10^8$	$1.76 \cdot 10^8$
B(Tesla)	3.10^{-4}	4.10^{-4}	5.10^{-4}	6.10^{-4}	10^{-3}
D (cm ² /s)	16.212	14.079	11.138	9.934	8.108
Topt (K)	257	290	318	343	424
Hopt (cm)	0.0095	0.009	0.0083	0.008	0.0075

Figures. 4, 5, and 6, are the plots of solar cell base optimum thickness as function respectively, of maximum diffusion coefficient, temperature and magnetic field.

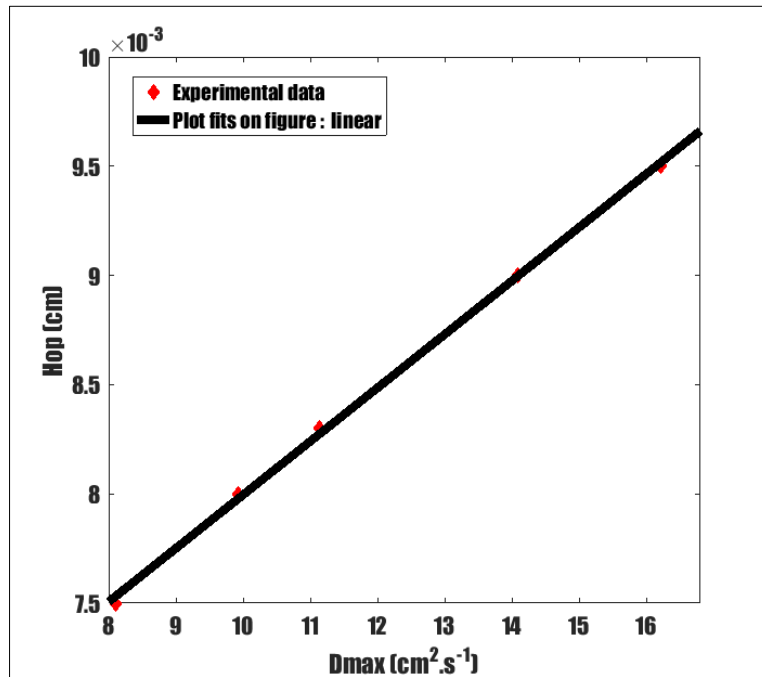


Figure 4 Optimum thickness versus Dmax

Figure. 4 gives the plot of the base optimum thickness, versus maximum diffusion coefficient, deduced from table. 2, and the modeling relationship is as follow:

$$Hop(cm) = 2.4 \cdot 10^{-4} \times Dmax + 0.0055 \dots\dots\dots (21)$$

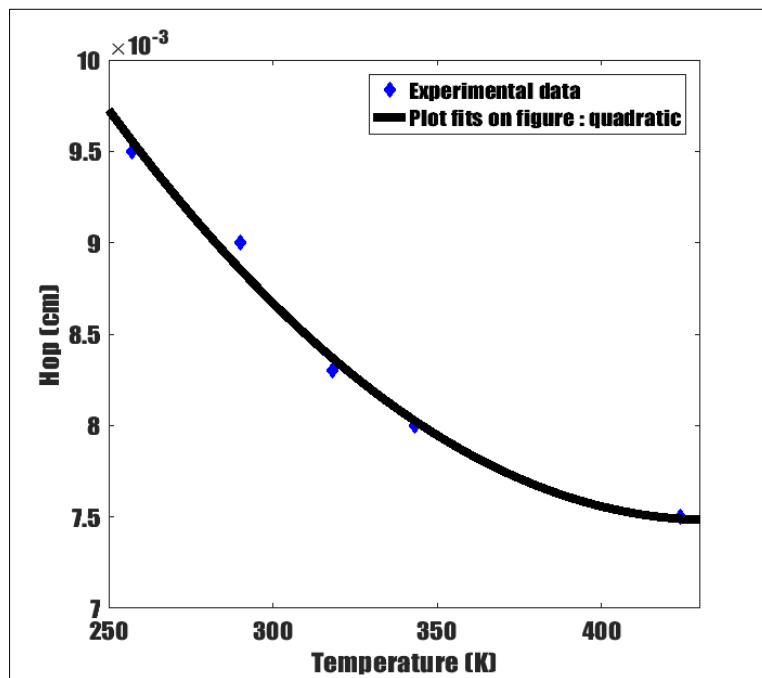


Figure 5 Optimum thickness versus temperature

From figure. 5, base optimum as fitted and gives the following relation:

$$Hop_t(cm) = 6.7 \cdot 10^{-8} \times T^2 - 5.8 \cdot 10^{-5} \times T + 0.02 \dots\dots\dots (22)$$

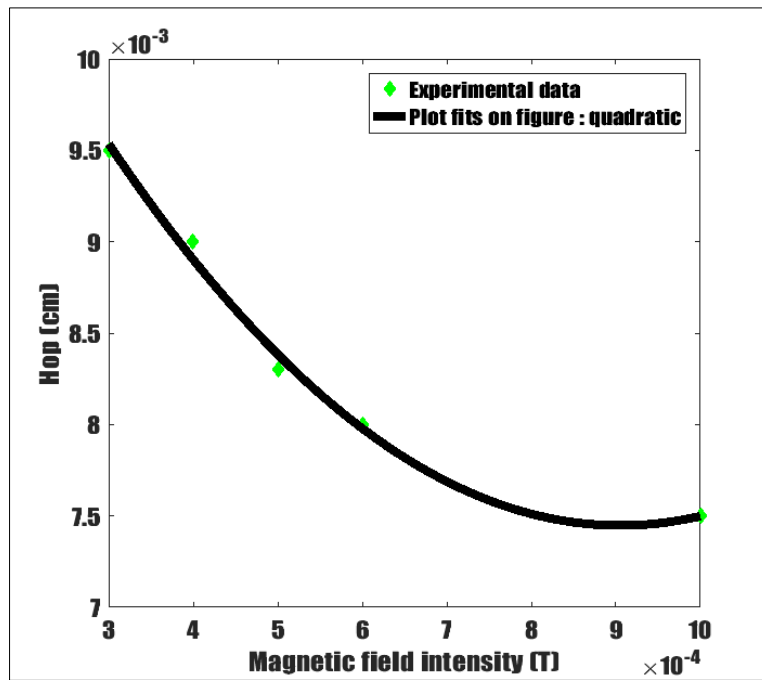


Figure 6 Optimum thickness versus magnetic field intensity

Figure. 6, gives the modeling relationship as:

$$Hop = 5.7 \cdot 10^3 \times B^2 - 10 \times B + 0.012 \dots\dots\dots (23)$$

4 Discussions

- A high absorption leads to a low penetration of light (alfa grand) so a generation near the junction (therefore short distance to travel before arriving at the junction [29].
- A high modulation frequency ($\omega\tau \gg 1$) causes the density of the photo generated carriers to be reduced towards the incident surface of the illumination, thus near the junction [13, 19, 53, 54].
- From sections a) and b), it appears that the Lorentz forces have a small effect on charge carriers with a short path to perform. [30], because deflection is not enough to slow down their collection to participate in the photocurrent.
- Thermal agitation by temperature rise (Umklapp) shows a decrease in the diffusion coefficient (Table. 2), which is therefore associated with a low diffusion length.

Other recent works have produced results that corroborate this trend of decreasing the optimum thickness of the silicon solar cell base with external factors:

- Under monochromatic illumination in frequency modulation, by the front [17] and rear [2, 13], or on vertical junctions connected in series [19].
- Under polychromatic illumination in frequency modulation by the front surface [5] and with effect of temperature [51, 62] or applied magnetic field [41].
- Under polychromatic illumination, by the front face or on vertical junctions connected in series and with effect of the magnetic field applied [14, 63, 64].
- Under polychromatic illumination, by the front face with effect of temperature and magnetic field [15, 36].

The thicknesses obtained were modeled according to these external parameters, as decreasing functions, thus showing a gain in material.

It emerges from the analysis of the physical mechanisms that control the optimization of the thickness of the base of the silicon solar cell [44, 46, 49, 50], that investigations on thin films [9, 23, 65, 66, 67] would lead to appreciable results and allowing a gain in material economy.

5 Conclusion

The magneto-transport equation relating to the density of the minority charge carriers in the base of the silicon solar ($n^+/p/p^+$), under monochromatic illumination, in frequency modulation, has been solved.

The profile of the dynamic photocurrent as a function of the recombination velocity at the junction, was represented, for different values of the diffusion coefficient of the excess minority carriers in the base, at temperature and frequency, both in a resonance situation.

This representation made it possible to deduce the expressions of the dynamic recombination velocity of the minority carriers on the back side of the base, depending on the diffusion parameters with the values of resonance and absorption of high value, for a low penetration of the illumination.

The graphical representation of these expressions on a two-axis curve, for different values of the diffusion coefficient in a resonance situation, made it possible to extract the optimum thickness of the base. The latter is represented as a function of the diffusion coefficient, the temperature and the magnetic field applied, for a high value of the absorption coefficient.

The analysis and mathematical modeling of these curves, give an optimum thickness growth as a function of the diffusion coefficient and a decrease as a function of temperature and magnetic field, from which we can deduce the possibility of reduction of the thickness in the manufacture of the solar cell by considering an economy of silicon material.

Compliance with ethical standards

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Disclosure of conflict of interest

The authors declare no conflicts of interest.

References

- [1] Diop, M. , Ba, H. , Thiam, N. , Diatta, I. , Traore, Y. , Ba, M. , Sow, E. , Mballo, O. and Sissoko, G. (2019) Surface Recombination Concept as Applied to Determinate Silicon Solar Cell Base Optimum Thickness with Doping Level Effect. *World Journal of Condensed Matter Physics*, 9, 102-111. doi: 10.4236/wjcmp.2019.94008.
- [2] M. Sall, M. F. MB. Fall, O. Diasse, G. Diop, I. Diatta, O. Dia, K. Loum, M. Wade and Sissoko, G. Determination of the optimum thickness of the base of the $n^+/p/p^+$ silicon solar cell, illuminated by the rear face by a monochromatic light of long wavelength in frequency modulation. *Journal of Chemical, Biological and Physical Sciences. JCBPS; Section C; November 2021 –January 2022, Vol. 12, No. 1; 064-077. DOI :10.24214/jcbps.C.11.4.07891.]*
- [3] R.Van Steenwinkel, M.C. Carotta, G. Martinelli, M. Mercli, L. Passari and D. Palmeri (1990). Lifetime Measurement in Solar Cell of Various Thickness and Related Silicon Wafer. *Solar Cells*, 28, 287-292. [https://doi.org/10.1016/0379-6787\(90\)90063-BG](https://doi.org/10.1016/0379-6787(90)90063-BG).
- [4] Luc, B., Shahriar, M., Dean, H., Marco, S., Manuela, A. and Claudio, N. (1994). Investigation of Carrier Transport through Silicon Wafers by Photocurrent Measurement. *Journal of Applied Physics*, 75, 4000-4008. <https://doi.org/10.1063/1.356022>
- [5] M.Kunst and A. Sanders. Transport of Excess Carriers in Silicon Wafers. *Semiconductor Science and Technology*, 1992, 7, 51-59. <https://doi.org/10.1088/0268-1242/7/1/009>

- [6] N.Honma and C. Munakata (1987). Sample Thickness Dependence of Minority Carrier Lifetimes Measured Using an ac Photovoltaic Method. *Japanese Journal of Applied Physics*, 26, 2033-2036. <https://doi.org/10.1143/JJAP.26.2033>
- [7] Demesmaeker, E., Symons, J., Nijs, J. and Mertens, R. (1991). The Influence of Surface Recombination on the Limiting Efficiency and Optimum Thickness of Silicon Solar Cells. 10th European Photovoltaic Solar Energy Conference, Lisbon, 8-12 April 1991, 66-67. https://doi.org/10.1007/978-94-011-3622-8_17
- [8] E. Sow, S. Mbodji, B. Zouma, M. Zoungrana, I. Zerbo, A. Sere & G. Sissoko (2012). Using Gauss Law in determining the width emitter extension region of the solar cell operating in open circuit condition. *Global Journal of Science Frontier Research Physics and Space Sciences Volume 12 Issue 6 Version 1.0*, p67-72, Year 2012. Online ISSN: 2249-4626 & Print ISSN: 0975-5896
- [9] A. A. Sayem, Y. Arafat and M. M. Rahman (2014). Thickness optimization and composition grading effect in heterojunction CIGS Solar Cell. 8th International Conference on Electrical and Computer Engineering (20-20 Dec, Dhaka, Bangladesh), 2014, pp. 524-527, doi: 10.1109/ICECE.2014.7026952.
- [10] Chen H. R, Lee. C. P, Chang. C. Y, Tsang. J. S, Tsai. K. L (2009). The study of emitter thickness effect on the heterostructure emitter bipolar transistors. *Journal of Applied Physics*, 74 (2), 1398-1402.
- [11] E.Gaubas and J. Vanhellemont (1996). A simple Technique for the Separation of Bulk and Surface Recombination Parameters in Silicon. *Journal of Applied Physics*, 80, 6293-6297. <https://doi.org/10.1063/1.363705M>
- [12] Navruz, T.S. and Saritas, M. (2012) Determination of the Optimum Material Parameters for Intermediate Band Solar Cells Diffusion Model. *Progress in Photovoltaics Research and Applications*, 22, 593-602. <https://doi.org/10.1002/pip.2283>
- [13] Sall, M, Diarisso .D ,Faty Mbaye Fall. M, Diop. G, Ndiaye. M, Loum/ K and Sissoko, G. (2021). Back Illuminated N/P/P+ Bifacial Silicon Solar Cell under Modulated Short-Wavelength: Determination of Base Optimum Thickness. *Energy and Power Engineering*, 13, 207-220. doi: 10.4236/epe.2021.135014
- [14] Sidi Dede, M. , Lamine Ba, M. , Amadou Ba, M. , Ndiaye, M. , Gueye, S. , Sow, E. , Diatta, I. , Diop, M. , Wade, M. and Sissoko, G. (2020) Back Surface Recombination Velocity Dependent of Absorption Coefficient as Applied to Determine Base Optimum Thickness of an n+/p/p+ Silicon Solar Cell. *Energy and Power Engineering*, 12, 445-458. doi: 10.4236/epe.2020.127027
- [15] Maimouna Mint ELY, Ndeye Thiam , Mor Ndiaye , Youssou Traore, Richard Mane , El hadji Sow , Oulimata mballo , Masse Samba Dieng, Cheikh Tidiane Sarr , Ibrahima Ly, Gregoire Sissoko, (2020) Surface recombination velocity concept as applied to determinate back surface illuminated silicon solar cell base optimum thickness, under temperature and external magnetic field effects. *Journal of Scientific and Engineering Research*, 7(2):69-77, <https://jsaer.com/archive/volume-7-issue-2-2020/>
- [16] Diop, G., Ba, H.Y., Thiam, N., Traore, Y., Dione, B., Ba, M.A., Diop, P., Diop, M.S., Mballo, O. and Sissoko, G. (2019). Base Thickness Optimization of a Vertical Series Junction Silicon Solar Cell under Magnetic Field by the Concept of Back Surface Recombination Velocity of Minority Carrier. *ARPN Journal of Engineering and Applied Sciences*, 14, 4078-4085.
- [17] Ndiaye, A., Gueye, S. , Sow, O. , Diop, G. , Ba, A. , Ba, M. , Diatta, I. , Habiboullah, L. and Sissoko, G. (2020). A.C. Recombination Velocity as Applied to Determine n+/p/p+ Silicon Solar Cell Base Optimum Thickness. *Energy and Power Engineering*, 12, 543-554. doi: 10.4236/epe.2020.1210033.
- [18] Gilbert Ndiasse Dione, Hamet Yoro BA, Gora Diop, Malick Ndiaye, Ibrahima Diatta, Khady Loum, Youssou Traore, Moustapha Thiame, Ousmane Sow, Mamadou Wade and S. Gregoire. Bifacial (n + -p-p +) Silicon Solar Cell base thickness optimization, while illuminated by the rear face with monochromatic light of short wavelenths. *International Journal of advanced Research (IJAR)*, 2022, 10(09), 409-418. <https://doi.org/10.21474/IJAR01/15372>
- [19] Malick Ndiaye, Ousmane Sow, Ibrahima Diatta, Gora Diop, Dibor Faye, KhadyLoum, YoussouTraore, MoustaphaThiame, Mamadou Wade And GregoireSissoko (2022). Optimization of the thickness of the doping rate base (Nb) of the (n+/p/p+) silicon solar cell with vertical multi-junction connected in series and placed under monochromatic illumination in frequency modulation. *Journal of Chemical, Biological and Physical Sciences*, Vol. 12, NO 4, 266-280. <https://doi.org/10.24214/jcbps.C.12.4.26680>

- [20] Le Quang Nam, M. Rodot, M. Ghannam, J. Cppy, P. de Schepper, J. Nijs, (1992). Solar Cells with 15.6% efficiency on multicrystalline silicone, using impurity gettering, back surface field and emitter passivation. *Int. J. Solar Energy*. Vol. 11, pp.273-279.
- [21] Fossum. J.G (1977). Physical Operation of Back-Surface-Field Silicon Solar Cells. *IEEE Transactions on Electron Devices*, 2, 322-325. <https://doi.org/10.1109/T-ED.1977.18735>
- [22] D.L.Meier, J.M. Hwang and R.B.Campbell (1988). The Effect of Doping Density and Injection Level on Minority Carrier Lifetime as Applied to Bifacial Dendritic Web Silicon Solar Cells. *IEEE Transactions on Electron Devices*, 35, 70-79. <https://doi.org/10.1109/16.2417>
- [23] Chung F; Chung-Feng Jeffery Kuo, Hung-Min Tu, Shin-Wei Liang, Wei-Lun Tsai (2010). Optimization of microcrystalline silicon thin film solar cell isolation processing parameters using ultraviolet laser. *Optics & Laser Technology*, Vol. 42 issue 6, Pp. 945-955. <http://dx.doi.org/10.1016/j.optlastec.2010.01.013>
- [24] R. R. Vardanyan, U. Kerst, B. Tierock, H. G. Wagemann (1997). Measurement of recombination parameters of solar cell in a magnetic field. *Proceeding of the 14th European Photovoltaic Solar Energy Conference (Barcelona, Spain)*. Pp 2367-2369.
- [25] Mandelis, A., Ward, A. and Lee, K.T. (1989). Combined AC Photocurrent and Photothermal Reflectance Response Theory of Semiconducting p-n Junctions. *Journal of Applied Physics*, 66, 5572-5583. <https://doi.org/10.1063/1.343662>
- [26] S.Gupta, P. Ahmed and S.Garg, (1988). A Method for the Determination of the Material parameters D, L, S and α from Measured Short-Circuit Photocurrent. *Solar Cells*, 25, 61-72. [https://doi.org/10.1016/0379-6787\(88\)90058-0P](https://doi.org/10.1016/0379-6787(88)90058-0P).
- [27] M. A. Green and M. Keevers, Optical Properties of Intrinsic Silicon at 300K. *Progress in Photovoltaics*, 1995, 3, 189-192. <http://dx.doi.org/10.1002/pip.4670030303>
- [28] Rajman, K., Singh, R. and Shewchun, J. (1979) Absorption Coefficient for Solar Cell Calculations. *Solid State Electronics*, 22, 793-795. [https://doi.org/10.1016/0038-1101\(79\)90128-X](https://doi.org/10.1016/0038-1101(79)90128-X)
- [29] U. C. Ray and S. K. Agarwal (1988). Wavelength Dependence of Short-Circuit Current Decay in Solar Cells. *J. Appl. Phys.* 63 (2), pp. 547-549.
- [30] Betser, Y., Ritter, D., Bahir, G., Cohen, S. and Serling, J. (1995). Measurement of the Minority Carrier Mobility in the Base of Heterojunction Bipolar Transistors Using a Magneto Transport Method. *Applied Physics Letters*, 67, 1883-1884. <https://doi.org/10.1063/1.114364>
- [31] F. Toure, M. Zoungrana, B. Zouma, S. Mbodji, S. Gueye, A. Diao & G. Sissoko (2012). Influence of Magnetic Field on Electrical Model and Electrical Parameters of a Solar Cell Under Intense Multispectral Illumination. *Global Journal of Science Frontier Research (A) Vol. XII, issue VI, Version I*, pp 51-59.
- [32] Flohr, Th. and Helbig, R. (1989). Determination of Minority-Carrier Lifetime and Surface Recombination Velocity by Optical-Beam-Induced-Current Measurements at Different Light Wavelengths. *Journal of Applied Physics*, 66, 3060-3065. <https://doi.org/10.1063/1.344161>
- [33] P. Singh, S.N. Singh, M. Lal, M. Husain (2008). Temperature dependence of I-V characteristics and performance parameters of silicon solar cell. , *Solar Energy Materials & Solar Cells*, 92, pp.1611–1616.
- [34] I. Diatta, I. Ly, M. Wade, M. S. Diouf, S. Mbodji, G. Sissoko, (2017) Temperature Effect on Capacitance of a Silicon Solar Cell under Constant White Biased Light. *World Journal of Condensed Matter Physics*, 6, pp.261-268.
- [35] Richard Mane, Ibrahima Ly, Mamadou Wade, IbrahimaDatta, Marcel S. Douf, YoussouTraore, MorNdiaye, SeniTamba, GrégoireSissoko (2017). Minority Carrier Diffusion Coefficient $D^*(B, T)$: Study in Temperature on a Silicon Solar Cell under Magnetic Field. *Energy and Power Engineering*, 9, pp.1-10 <http://www.scirp.org/journal/epe>
- [36] Sega Diagne, Ousmane Sow, Gora Diop, Richard Mane, IbrahimaDiatta, DjibyNdiongue ,YoussouTraore, LemrabottHabiboullahMamadou Wade and GregoireSissoko. (2022) Optimization of silicon solar cell base thickness, while illuminated by a long wavelength monochromatic light: influence of both Lorentz law and Umclapp process. *International Journal of Advanced Research*, 10(08), 133-143. <http://dx.doi.org/10.21474/IJAR01/151508>

- [37] Wafaa Abd El-Basit, Ashraf Mosleh Abd El-Maksood and Fouad Abd El-Moniem Saad Soliman (2013). Mathematical Model for Photovoltaic Cells. Leonardo Journal of Sciences, Issue 23, pp.13-28. (<http://ljs.academicdirect.org/>)
- [38] Dorkel, J.M. and Leturcq, P. (1981) Carrier Mobilities in Silicon Solar Semi-Empirically Related Temperature, Doping and Injection Level. Solid State Electron, 24, 821-825. [https://doi.org/10.1016/0038-1101\(81\)90097-6](https://doi.org/10.1016/0038-1101(81)90097-6)
- [39] Dieng, A., Zerbo, I., Wade, M., Maiga, A.S. and Sissoko, G. (2011). Three-Dimensional Study of a Polycrystalline Silicon Solar Cell: The Influence of the Applied Magnetic Field on the Electrical Parameters. Semiconductor Science and Technology, 26, Article ID: 095023. <http://dx.doi.org/10.1088/0268-1242/26/9/095023>
- [40] Diao, A., Thiam, N., Zoungrana, M., Sahin, G., Ndiaye, M. and Sissoko, G. (2014) Diffusion Coefficient in Silicon Solar Cell with Applied Magnetic Field and under Frequency: Electric Equivalent Circuits. World Journal of Condensed Matter Physics, 4, 84-92. <https://doi.org/10.4236/wjcmp.2014.42013>
- [41] Amadou Mar Ndiaye, Sega Gueye, Mame Faty Mbaye Fall, Gora Diop, Amadou Mamour Ba, Mamadou Lamine Ba, Ibrahima Diatta, Lemrabott Habiboullah and G. Sissoko (2020). Diffusion Coefficient at Resonance Frequency as Applied to n+/p/p+ Silicon Solar Cell Optimum Base Thickness Determination. Journal of Electromagnetic Analysis and Applications, 12, 145-158. <http://doi.org/10.4236/jemaa.2020.1210012>
- [42] Seydina, D., Mor, N., Ndeye, T., Youssou, T., Mamadou, L.B., Ibrahima, D., Marcel, S.D., Oulimata, M., Amary, T. and Grégoire, S. (2019) Influence of Temperature and Frequency on Minority Carrier Diffusion Coefficient in a Silicon Solar Cell Under Magnetic Field. Energy and Power Engineering, 11, 355-361. <https://doi.org/10.4236/epe.2019.1110023>
- [43] De Vischere, P. (1986) Comment on G. J. Rees. "Surface Recombination Velocity— A Useful Concept?" Solid State Electronics, 29, 1161-1164. [https://doi.org/10.1016/0038-1101\(86\)90059-6](https://doi.org/10.1016/0038-1101(86)90059-6)
- [44] Sissoko, G., Museruka, C., Corréa, A., Gaye, I. and Ndiaye, A.L. (1996). Light Spectral Effect on Recombination Parameters of Silicon Solar Cell. Proceeding of the 4th World Renewable Energy Congress, (15-21 June). Denver, Colorado (Pergamon), Part III, pp.1487-1490.
- [45] Sissoko, G., Sivoththanam, S., Rodot, M. and Mialhe, P. (1992) Constant Illumination-Induced Open Circuit Voltage Decay (CIOVD) Method, as Applied to High Efficiency Si Solar Cells for Bulk and Back Surface Characterization. 11th European Photovoltaic Solar Energy Conference and Exhibition, Montreux, 12-16 October 1992, 352-354.
- [46] Ly, I., Ndiaye, M., Wade, M., Thiam, N., Sega, Gueye. And Sissoko, G. (2013) Sissoko Concept of Recombination Velocity Sfcc at the Junction of a Bifacial Silicon Solar Cell, in Steady State, Initiating the Short-Circuit Condition. Research Journal of Applied Sciences, Engineering and Technology, 5, 203-208. <https://doi.org/10.19026/rjaset.5.5105>
- [47] O. Diasse, R. S. Sam, H. L. Diallo, M. Ndiaye, N. Thiam, S. Mbodji and G. Sissoko (2012). Solar cell's classification by the determination of the specific values of the back surface recombination velocities in open circuit and short-circuit operating conditions. International Journal of Emerging Trends & Technology in Computer Science (IJETTCS), 2012, 2278/6856: (pp.18-23)
- [48] Ly Diallo, H., Wade, M., Ly, I., NDiaye, M., Dieng, B., Lemrabott, O.H., Maïga, A.S. and Sissoko, G. (2012). 1D Modeling of a Bifacial Silicon Solar Cell under Frequency Modulation, Monochromatic Illumination: Determination of the Equivalent Electrical Circuit Related to the Surface Recombination Velocity. Research Journal of Applied Sciences, Engineering and Technology, 4, 1672-1676. <http://www.maxwell.org>
- [49] H.L.Diallo, A.S. Maiga, A. Wereme and G. Sissoko, (2008). New Approach of both Junction and Back Surface Recombination Velocities in a 3D Modelling Study of a Polycrystalline Silicon Solar Cell. The European Physical Journal Applied Physics, 42, 193-211. <http://dx.doi.org/10.1051/epjap:2008085>
- [50] Diasse, O., Diao, A., Ly, I., Diouf, M.S., Diatta, I., Mane, R., Traore, Y. and Sissoko, G. (2018) Back Surface Recombination Velocity Modeling in White Biased Silicon Solar Cell under Steady State. Journal of Modern Physics, 9, 189-201. <https://doi.org/10.4236/jmp.2018.92012>
- [51] Mame Faty Mbaye Fall, Idrissa Gaye, Dianguina Diarrisso, Gora Diop, Khady Loum, Nafy Diop, Khalidou Mamadou Sy, Mor Ndiaye and G. Sissoko (2021). Ac back surface recombination velocity in n+/p/p+ silicon solar cell under monochromatic light and temperature. Journal of Electromagnetic Analysis and Applications, 13, 67-81. <http://doi.org/10.4236/jemaa.2021.135005>

- [52] Denise, K., Mamadou, L.B., Mamour, A.B., Gora, D., El Hadj, S., Oulimata, M. and Gregoire, S. (2020) AC Back Surface Recombination in $n^+ - p - p^+$ Silicon Solar Cell: Effect of Temperature. International Journal of advanced Research (IJAR), 8, 140-151. <https://doi.org/10.21474/IJAR01/11273>
- [53] Ly, I., Zerbo, I., Wade, M., Ndiaye, M., Dieng, A., Diao, A., Thiam, N., Thiam, A., Dione, M.M., Barro, F.I., Maiga, A.S. and Sissoko, G. (2011). Bifacial Silicon Solar Cell under Frequency Modulation and Monochromatic Illumination: Recombination Velocities and Associated Equivalent Electrical Circuits. Proceedings of 26th European Photovoltaic Solar Energy Conference and Exhibition, Hamburg, 5-9 September 2011, 298-301.
- [54] Zerbo, I., Barro, F.I., Mbow, B., Diao, A., Madougou, S., Zougmore, F. and Sissoko, G. (2004) Theoretical Study of Bifacial Silicon Solar Cell under Frequency Modulate white Light: Determination of Recombination Parameters. Proceedings of the 19th European Photovoltaic Solar Energy Conference, Paris, 7-11 June 2004, 258-261.
- [55] Thiam, N., Diao, A., Ndiaye, M., Dieng, A., Thiam, A., Sarr, M., Maiga, A.S. and Sissoko, G. (2012). Electric Equivalent Models of Intrinsic Recombination Velocities of a Bifacial Silicon Solar Cell under Frequency Modulation and Magnetic Field Effect. Research Journal of Applied Sciences, Engineering and Technology, 4, 4646-4655. <https://doi.org/10.19026/rjaset.5.4825>
- [56] Youssou Traore, Ndeye Thiam, Moustapha Thiame, Amary Thiam, Mamadou Lamine Ba, Marcel Sitor Diouf, Ibrahima Diatta, Oulymata Mballo, El Hadji Sow, Mamadou Wade, Grégoire Sissoko, (2019) AC Recombination Velocity in the Back Surface of a Lamella Silicon Solar Cell under Temperature. Journal of Modern Physics, 10, pp.1235-1246 <https://www.scirp.org/journal/jmp>
- [57] Gueye, M., Diallo, H.L., Moustapha, A.K.M., Traore, Y., Diatta, I. and Sissoko, G. (2018) Ac Recombination Velocity in a Lamella Silicon Solar Cell. World Journal of Condensed Matter Physics, 8, 185-196. <https://doi.org/10.4236/wjcmp.2018.84013>
- [58] Chih Hsin Wang and ArnostNeugroschel (1991).Minority-carrier lifetime and surface recombination velocity measurement by frequency-domain photoluminescence. IEEE transactions on electron devices, vol.38, no. 9, pp2169-2180.
- [59] Antilla, O.J. and Hahn, S.K. (1993). Study on Surface Photovoltage Measurement of Long Diffusion Length Silicon: Simulation Results. Journal of Applied Physics, 74, 558-569. <https://doi.org/10.1063/1.355343>
- [60] Stokes, E.D. and Chu, T.L. (1977). Diffusion Lengths in Solar Cells from Short-Circuit Current Measurements. Applied Physics Letters, 30, 425-426. <https://doi.org/10.1063/1.89433>
- [61] Muzeyyen Saritas and Harry D. Mckell (1988). Comparison of minority carrier diffusion length measurements in silicon by the photoconductive decay and surface photovoltage methods. J. Appl. Phys 63 (9) pp. 4561-67.
- [62] Francois Michel Ndiaye, Mamadou Lamine Ba, Mamour Amadou Ba, Gora Diop, Ibrahima Diatta, El Hadj Sow, Oulimata Mballo and Gregoire Sissoko, (2020). Lamella Silicon Optimum Width Determination Under Temperature. Int. J. Adv. Res. 8(06), 1409-1419.
- [63] Thiaw, C. , Ba, M. , Amadou Ba, M. , Diop, G. , Diatta, I. , Ndiaye, M. and Sissoko, G. (2020) $n^+ - p - p^+$ Silicon Solar Cell Base Optimum Thickness Determination under Magnetic Field. Journal of Electromagnetic Analysis and Applications, 12, 103-113. doi: 10.4236/jemaa.2020.127009.
- [64] Dibor Faye, Sega Gueye, Mor Ndiaye, Mamadou Lamine Ba, Ibrahima Diatta, Youssou Traore, Masse Samba Diop, Gora Diop, Amadou Diao and Gregoire Sissoko. Lamella Silicon Solar Cell under Both Temperature and Magnetic Field: Width Optimum Determination. Journal of Electromagnetic Analysis and Applications, 2020, 12, 43-55. <https://doi.org/10.4236/jemaa.2020.124005>
- [65] Bitnar, B., Glatthaar, R., Marckmann, C., Spiegel, M., Tölle, R., Fath, P., Willeke, G. and Bucher, E. (1998) Lifetime Investigations on Screen printed Silicon Solar Cells. Proceedings of the 2nd World Conference and Exhibition on Photovoltaic Solar Energy Conversion, 1362-1365.
- [66] Yasar S., Kahraman S., Cetinkaya S., Apaydin S., Bilican I., Uluer I. (2016). Numerical thickness optimization study of CIGS based solar cells with wxAMPS, Optik, 127 (20), pp. 8827-8835.
- [67] S. Kumar, V. Sareen, N. Batra, P. K. Singh (2010). Study of C-V characteristic in thin $n^+ - p - p^+$ silicon solar cells and induced junction $n - p - p^+$ cell structures. Solar Energy Materials and Solar Cells, 94, 1469-1472